

The Hierarchy Problem & Compositeness

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The Standard Model as an Effective Theory

with fundamental scale $\Lambda_{UV}^2 \gg 1 \text{ TeV}$

The Standard Model as an Effective Theory

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$$\mathcal{L}_{SM} = \mathcal{L}_{kin} + g A_\mu \bar{F} \gamma_\mu F + Y_{ij} \bar{F}_i H F_j + \lambda (H^\dagger H)^2$$

d=4

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$$\begin{aligned} &+ \frac{b_{ij}}{\Lambda_{UV}} L_i L_j H H \\ &+ \frac{c_{ijkl}}{\Lambda_{UV}^2} \bar{F}_i F_j \bar{F}_k F_\ell + \frac{c_{ij}}{\Lambda_{UV}} \bar{F}_i \sigma_{\mu\nu} F_j G^{\mu\nu} + \dots \\ &+ \dots \end{aligned}$$

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$\Lambda_{UV} \rightarrow \infty$ (pointlike limit) nicely accounts for ‘what we see’

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with fundamental scale $\Lambda_{UV}^2 \gg 1 \text{ TeV}$

$$+ c\Lambda_{UV}^2 H^\dagger H$$

d<4

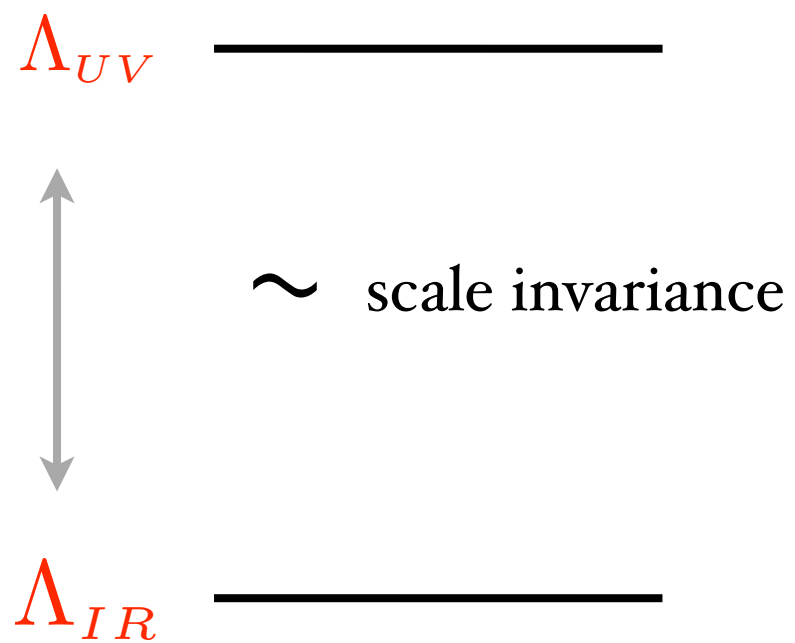
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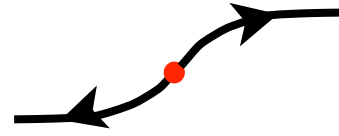
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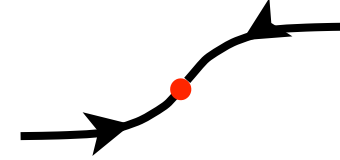
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hierarchy's naturalness $\longleftrightarrow$ fixed point stability



unstable

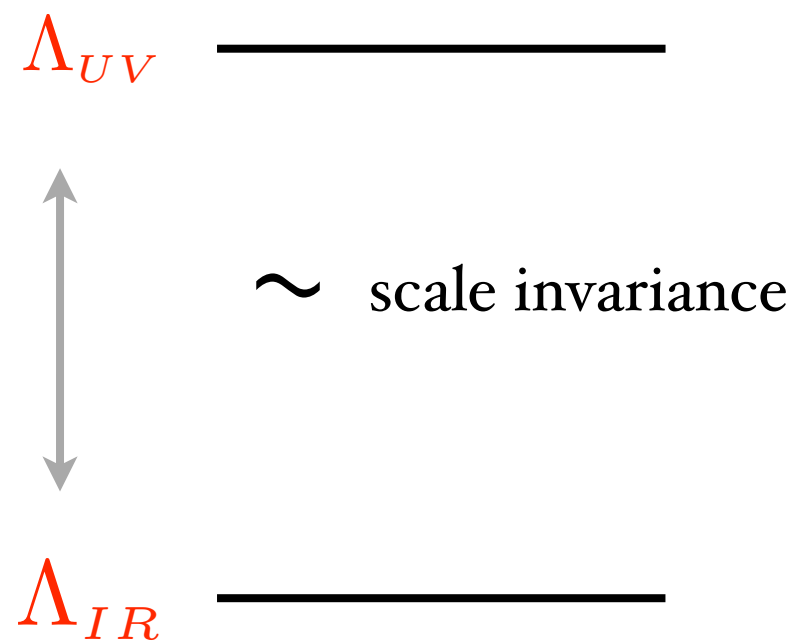


stable

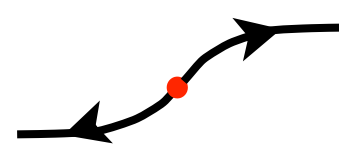


marginal

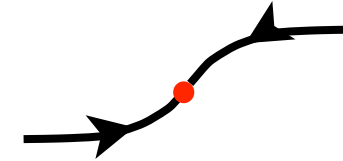
$m_H^2 \equiv$ ***strongly relevant*** perturbation



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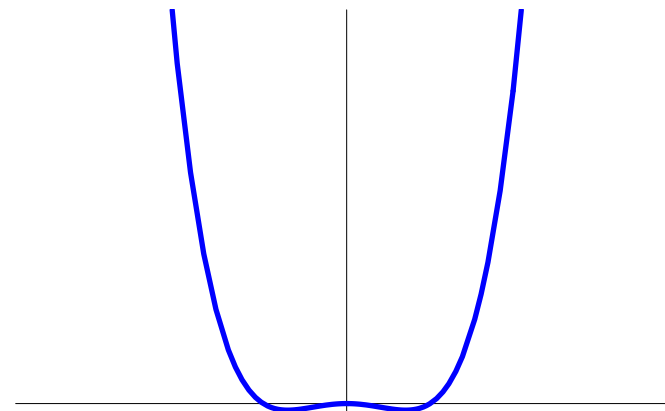


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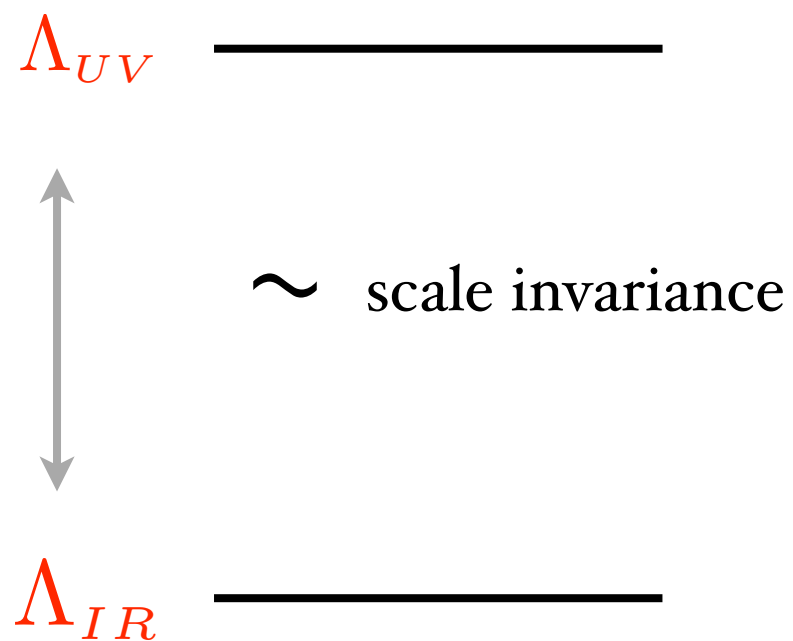


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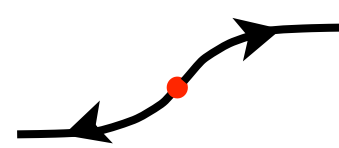
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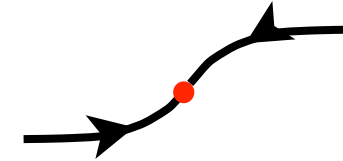
$$|T - T_c| \ll T$$



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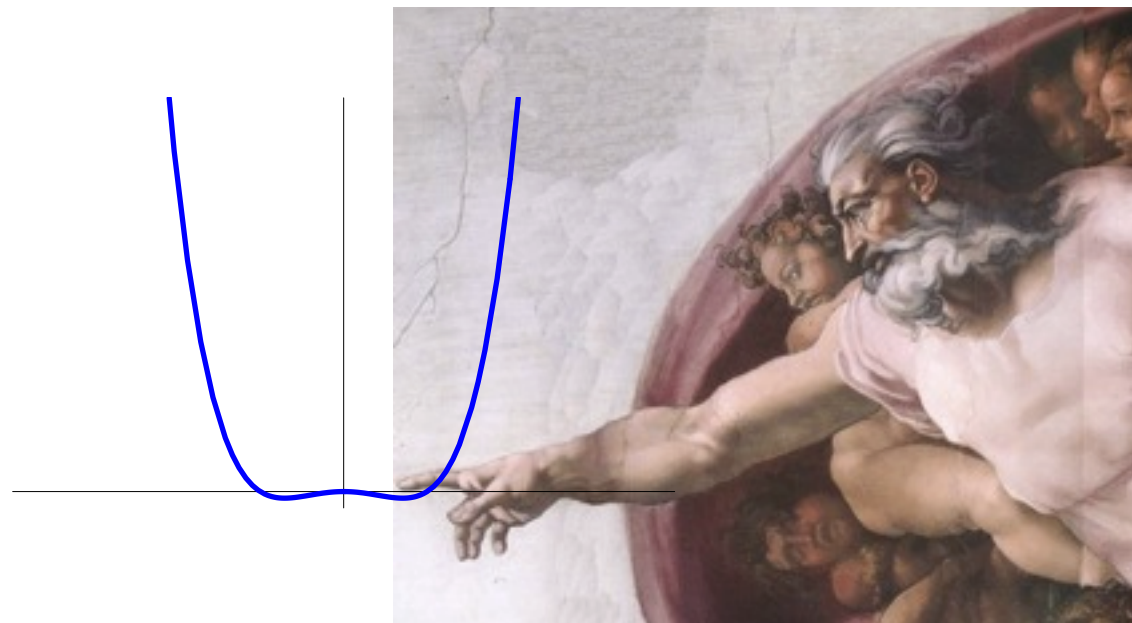


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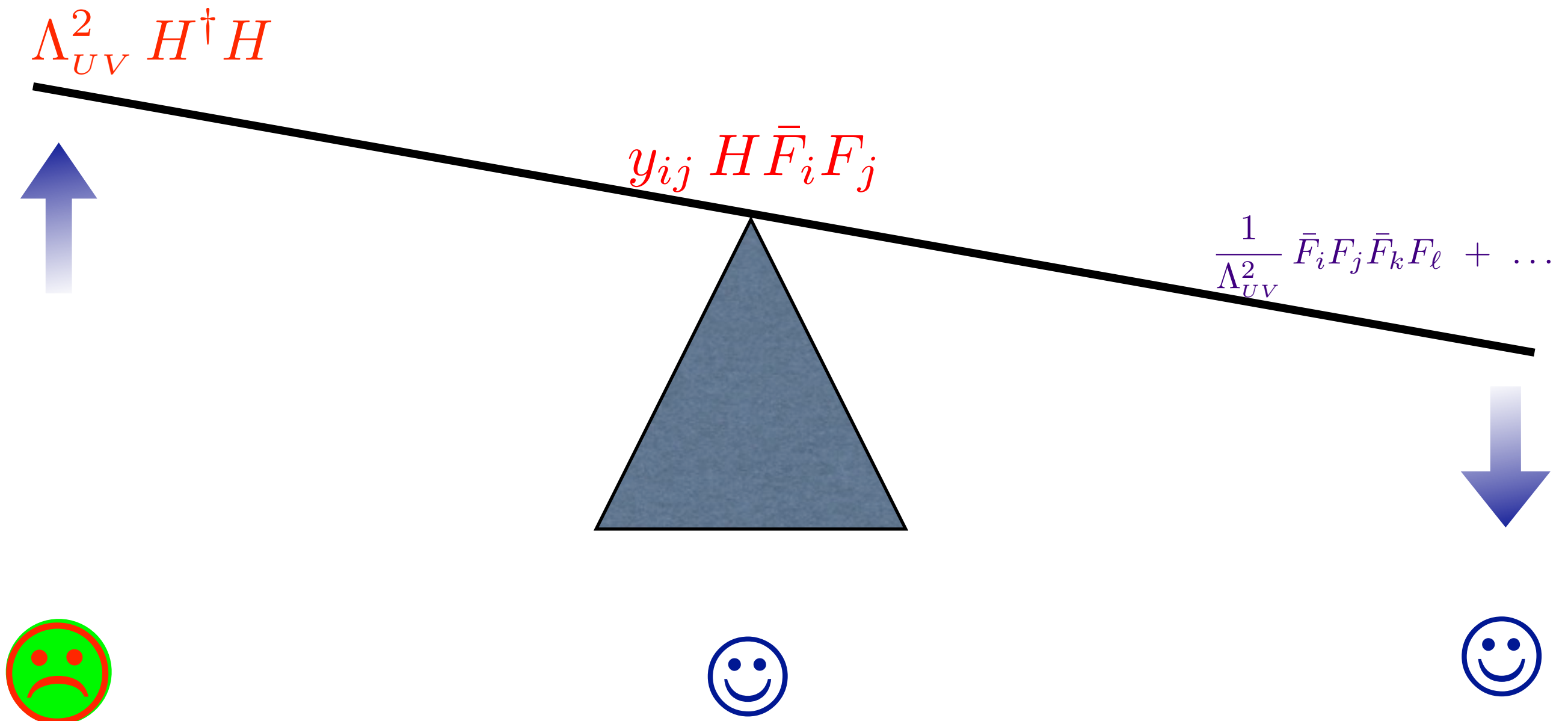
$$|T - T_c| \ll T$$



picture courtesy of V. Rychkov
who stole it anyway

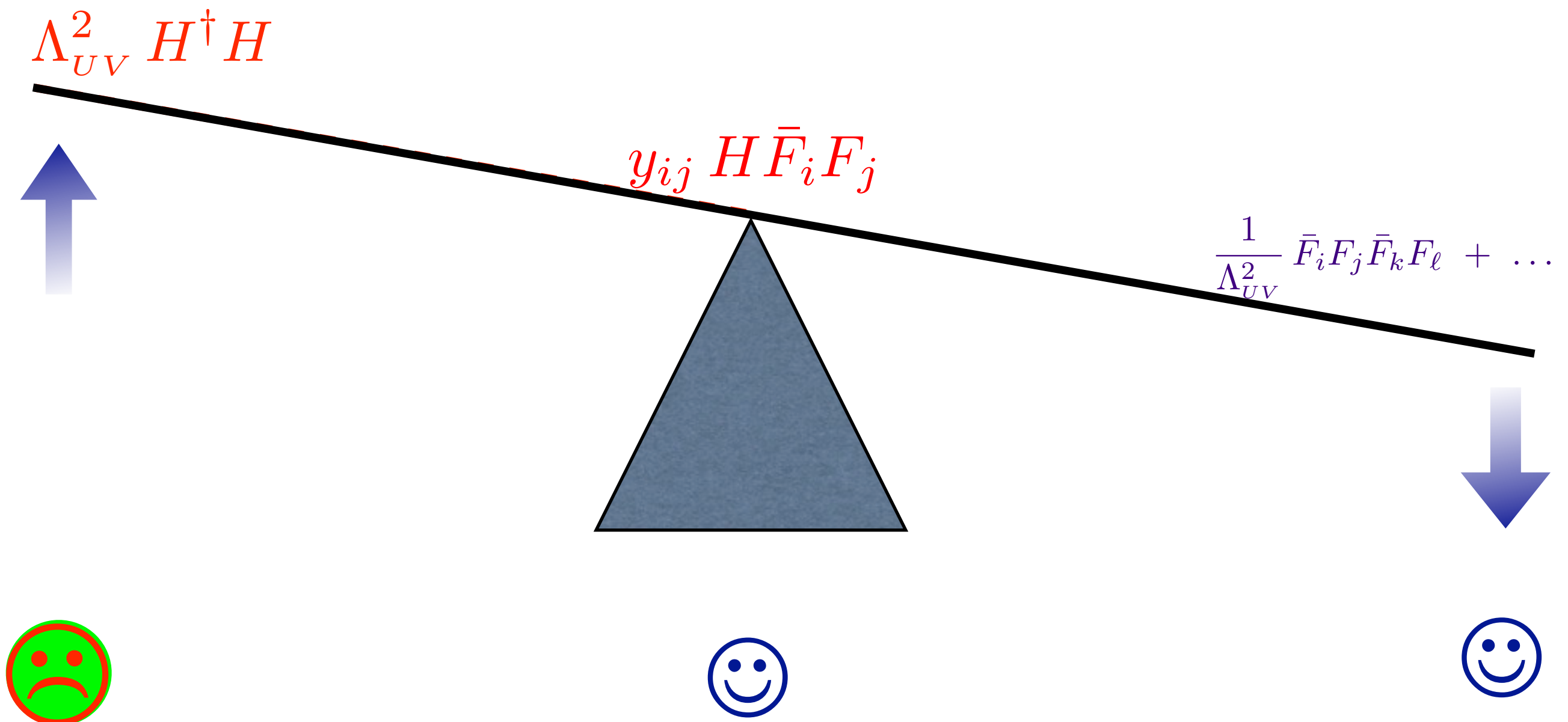
Hierarchy see-saw

Standard Model up to some $\Lambda_{UV}^2 \gg 1 \text{ TeV}$



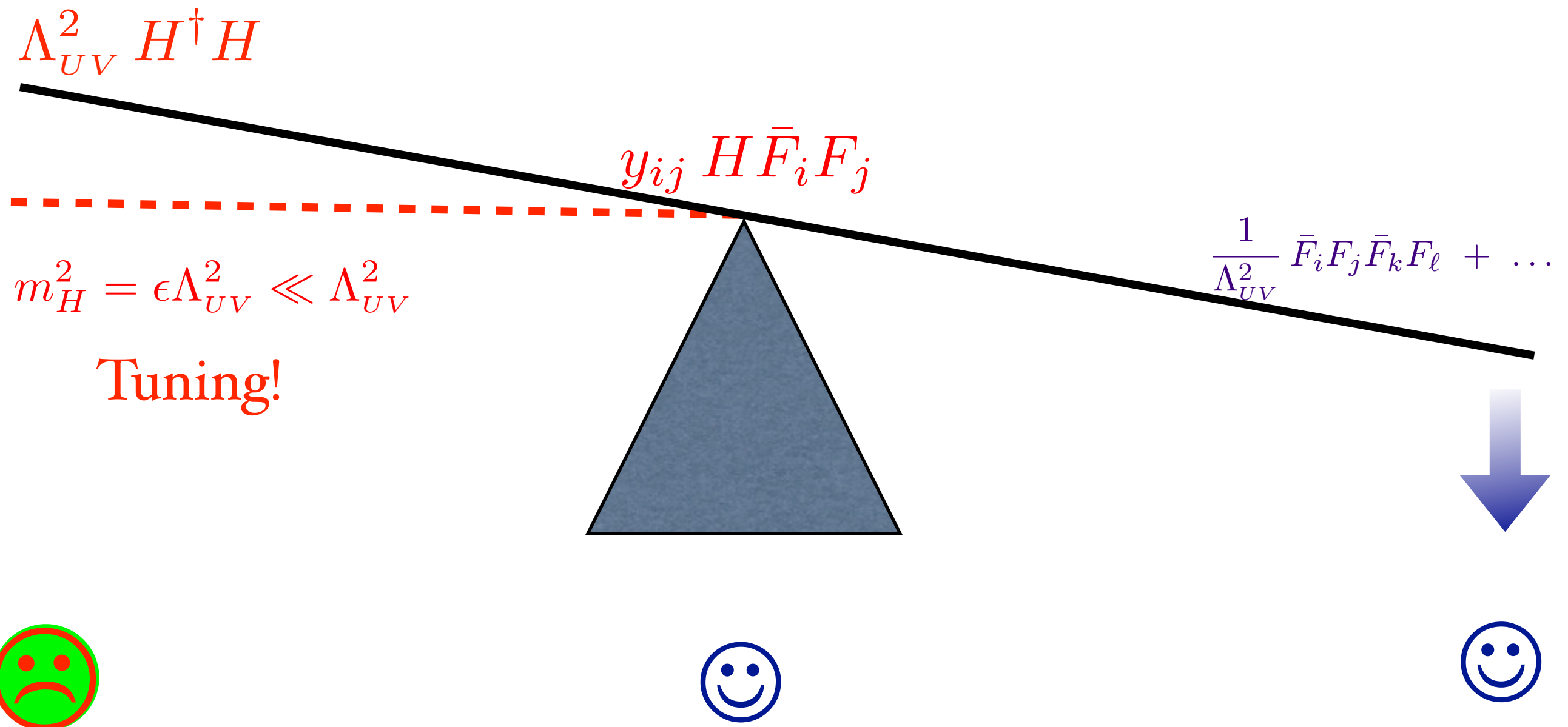
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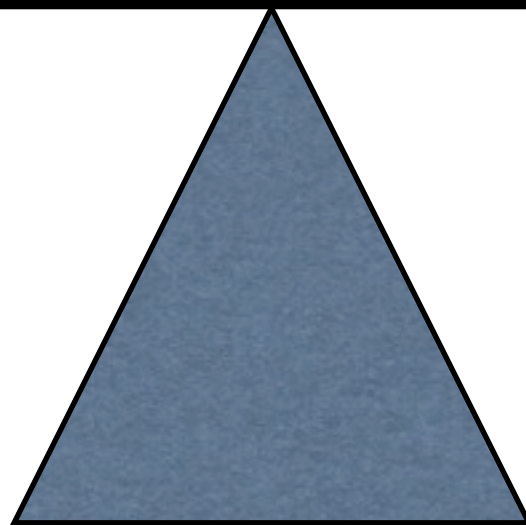


Natural SM : $\Lambda_{UV}^2 \lesssim 1 \text{ TeV}$

$$\Lambda_{UV}^2 H^\dagger H$$

$$y_{ij} H \bar{F}_i F_j$$

$$\frac{1}{\Lambda_{UV}^2} \bar{F}_i F_j \bar{F}_k F_\ell + \dots$$



Un-natural SM

The Higgs boson really is * The SM Higgs boson*

Flavor and approx B & L are theoretically appealing

... and experimentally boring

How would one understand the apparent tuning?

- Anthropic selection
- There is more than Effective Field Theory
- Intelligent design

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Natural SM

Supersymmetry

$$m^2 H^\dagger H$$

$$m^2 = 0 \quad \text{enhanced UV symmetry}$$

$$m^2 \neq 0$$

$$\text{new states at } g_W v_F \sim 100 \text{ GeV}$$

dimensional
transmutation

Compositeness

$$\dim(H^\dagger H) \geq 4$$

$$v_F \neq 0$$

$$\text{new states at } 4\pi v_F \sim 2 \text{ TeV}$$

In both cases, must use ingenuity to satisfy flavor and EW constraints

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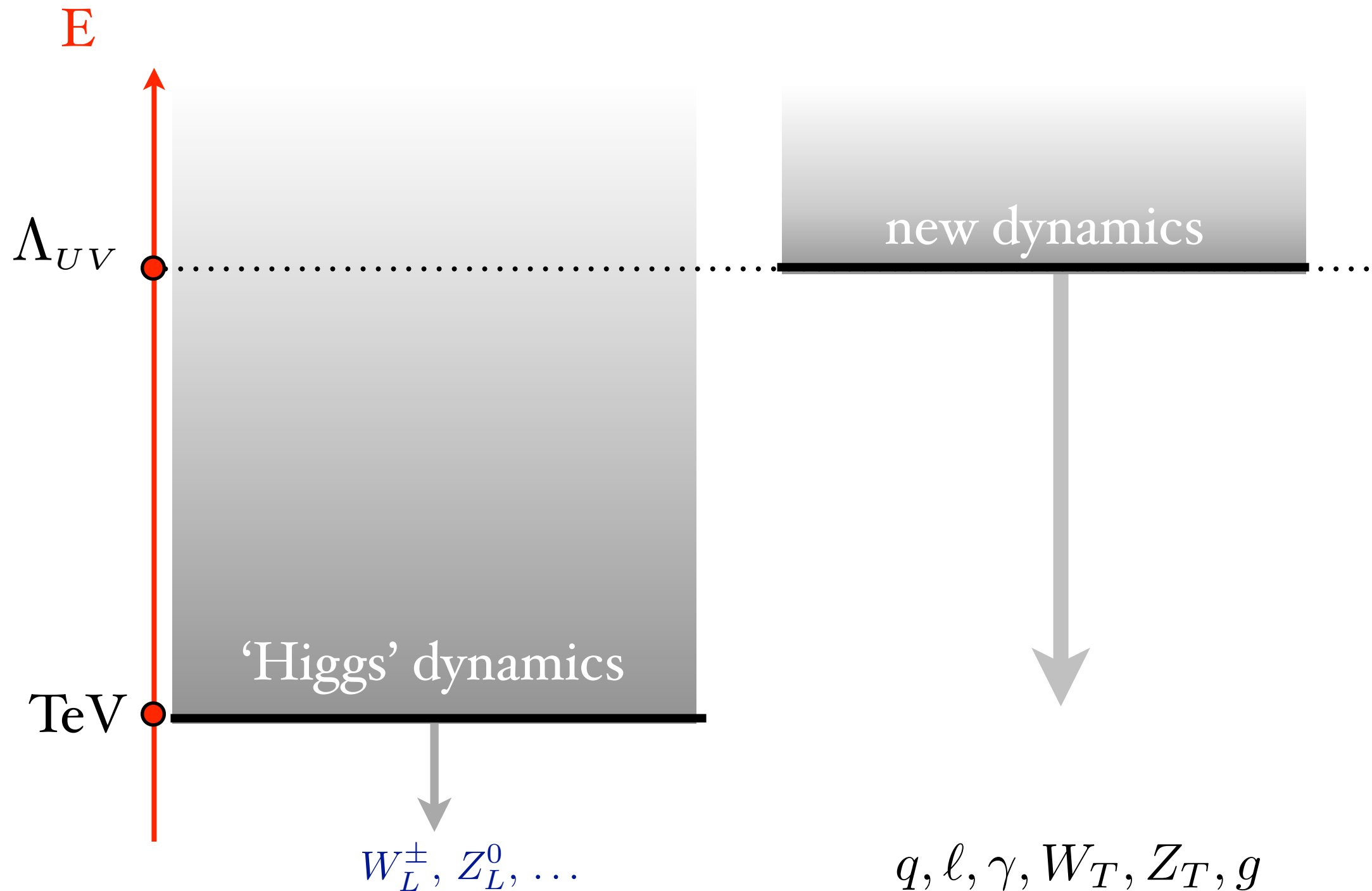
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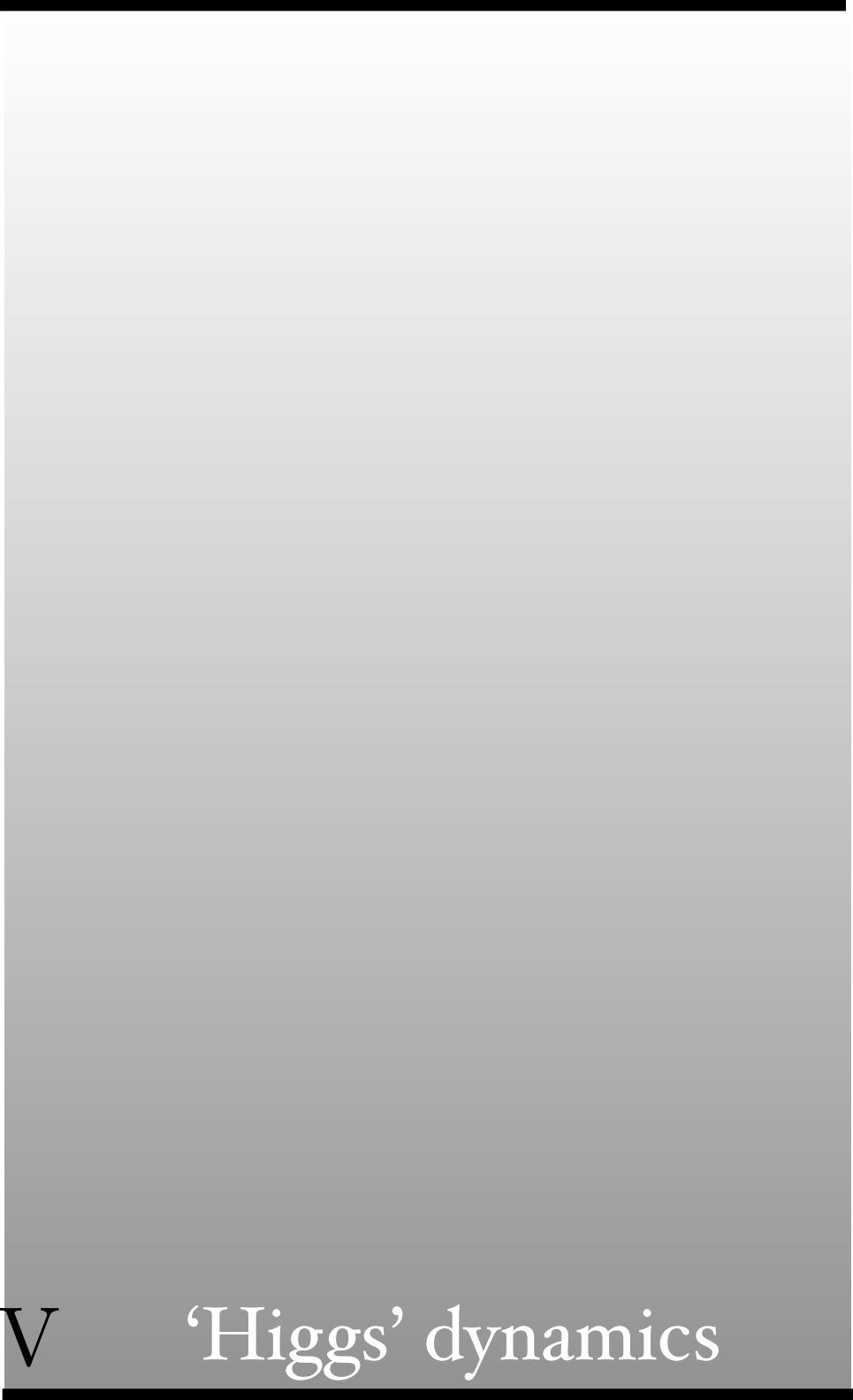
In both cases, must use ingenuity to satisfy flavor and EW constraints

Collider data display no signal of compositeness
for quarks, leptons and *transversely polarized* vector bosons

Plausible scenario



Λ_{UV}



Need $\Lambda_{UV} \gg \text{TeV}$
to filter out unwanted
effects and produce a
realistic Flavor story

Scale (conformal) invariant
theories are thus an essential
ingredient of model building

TeV 'Higgs' dynamics

Λ_{UV}



‘Higgs’ dynamics

TeV

80's : asymptotically free gauge theory
(Technicolor)

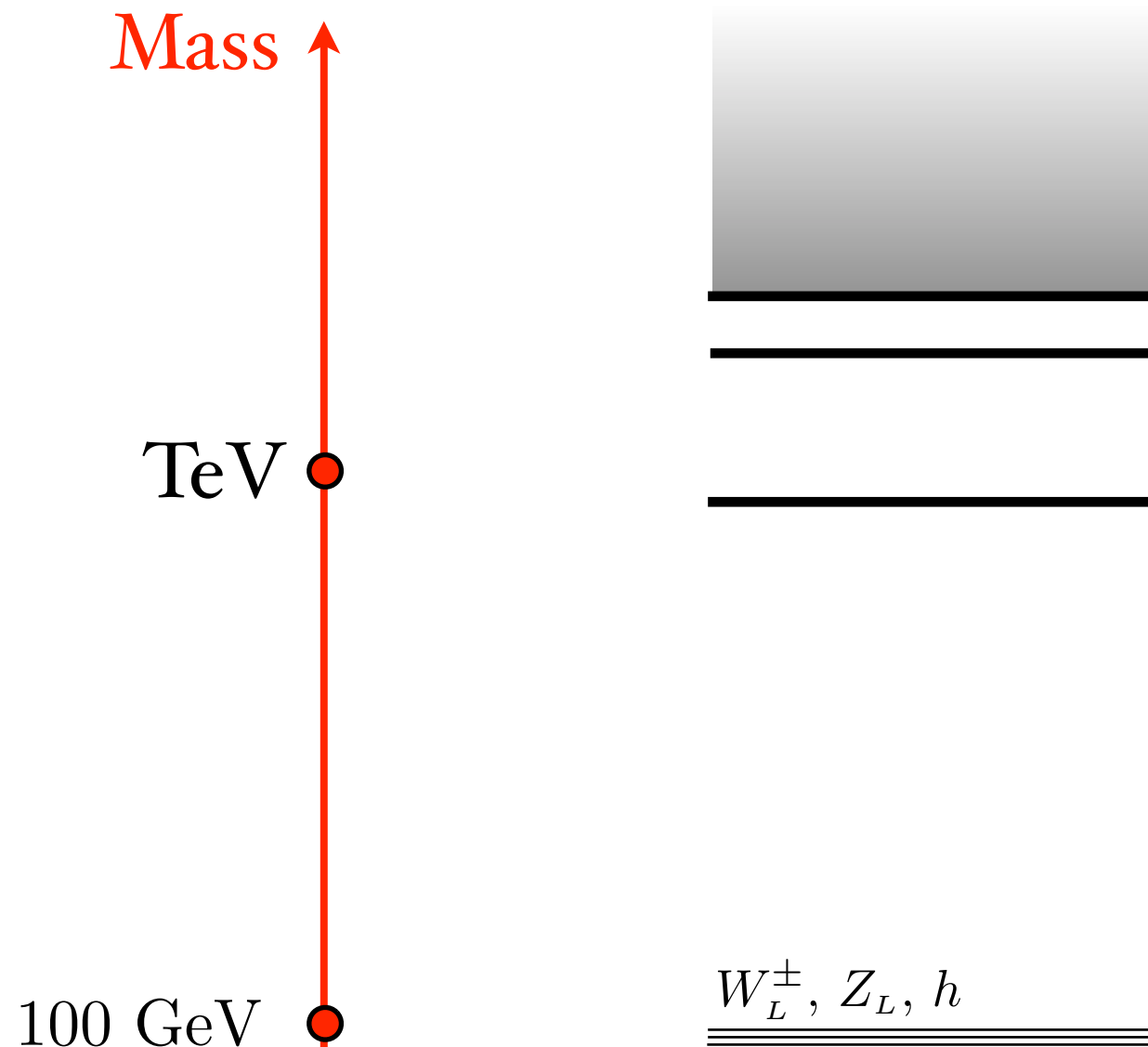
2000's : Holographic CFTs
(Randall-Sundrum)

‘Abstract CFT’

characterized by

- symmetry
- operator content

The structure underlying the Higgs sector



$$H = \begin{pmatrix} h_1 + ih_2 \\ h + ih_3 \end{pmatrix}$$

must be a pseudo-Golstone multiplet

Georgi, Kaplan '84
Banks '84

Arkani-Hamed, Cohen, Katz, Nelson '02
Agashe, Contino, Pomarol '04

Simplest options compatible with $\rho \simeq 1$

$$SO(5)/SO(4) \longrightarrow H$$

$$SO(6)/SO(5) \longrightarrow H \oplus \eta$$

$$SO(6)/SO(4) \times U(1) \longrightarrow H_1 \oplus H_2$$

$$SO(4, 1)/SO(4) \longrightarrow H$$

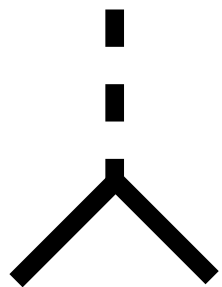
Composite sector is *broadly* described by:

Giudice, Grojean, Pomarol, RR, 2007

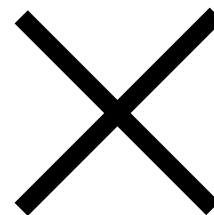
♦ one mass scale m_ρ (of order TeV)

♦ one coupling g_ρ $g_\rho \sim g_{KK}$ $g_\rho \sim \frac{4\pi}{\sqrt{N}}$

♦ decay constant $f \sim \frac{m_\rho}{g_\rho}$



$$= g_\rho \bar{\Psi} \Psi \Phi$$



$$= \frac{g_\rho^2}{m_\rho^2} \bar{\Psi} \Psi \bar{\Psi} \Psi$$

Origin of Higgs potential

strongly coupled
Higgs sector

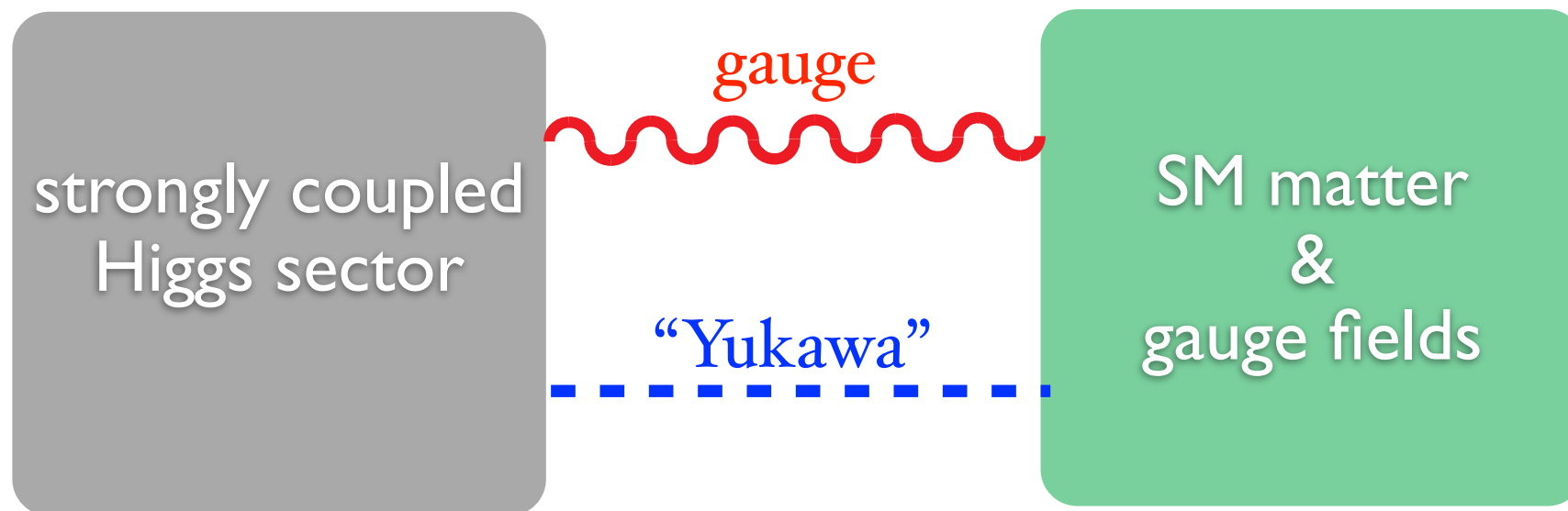
SM matter
&
gauge fields

global symmetry weakly broken

$$V(h) = \frac{m_\rho^4}{g_\rho^2} \times \frac{\lambda_t^2}{16\pi^2} \times F(h/f)$$

$$\sim \frac{\lambda_t^2}{16\pi^2} m_\rho^2 H^\dagger H + \frac{g_\rho^2}{16\pi^2} \lambda_t^2 (H^\dagger H)^2 + \dots$$

Origin of Higgs potential



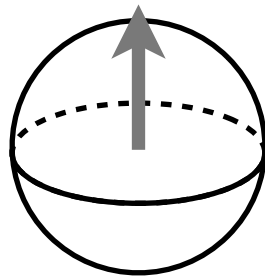
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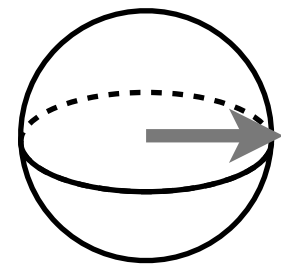
Vacuum
dynamics

unbroken $SU(2)_L \times U(1)$



$$v = 0$$

maximally broken



$$v = f$$

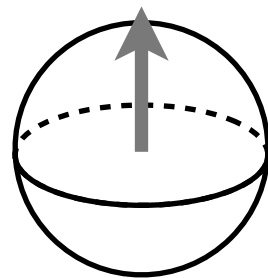
$$V \propto F(h/f) \quad \text{generically} \quad \frac{v^2}{f^2} = O(1)$$

EW precision
observables

$$\mathcal{O} \sim \frac{v^2}{f^2} \times \mathcal{O}_{\text{TechniColor}}$$

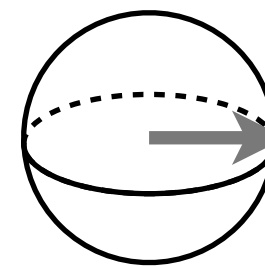
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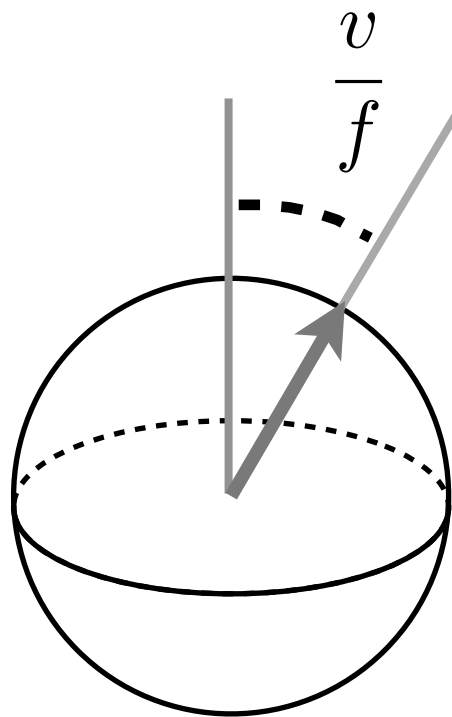
simply tune $\frac{v^2}{f^2} \sim 0.05 \div 0.1$

be clever : Little Higgs

EW precision
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Vacuum
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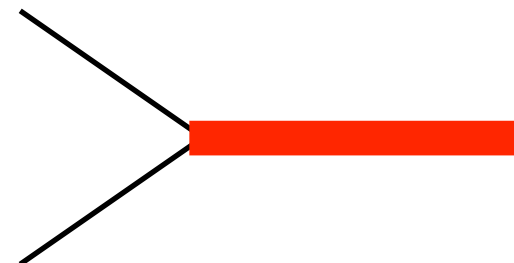
Two Ways to Flavor

Bilinear: ETC, conformalTC

Dimopoulos, Susskind
Holdom

....

Luty, Okui



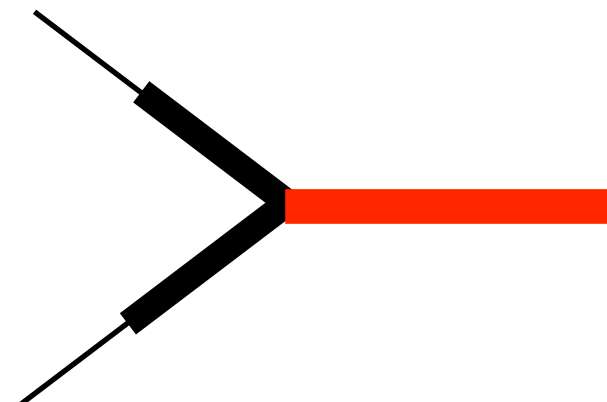
Linear: partial compositeness

D.B. Kaplan

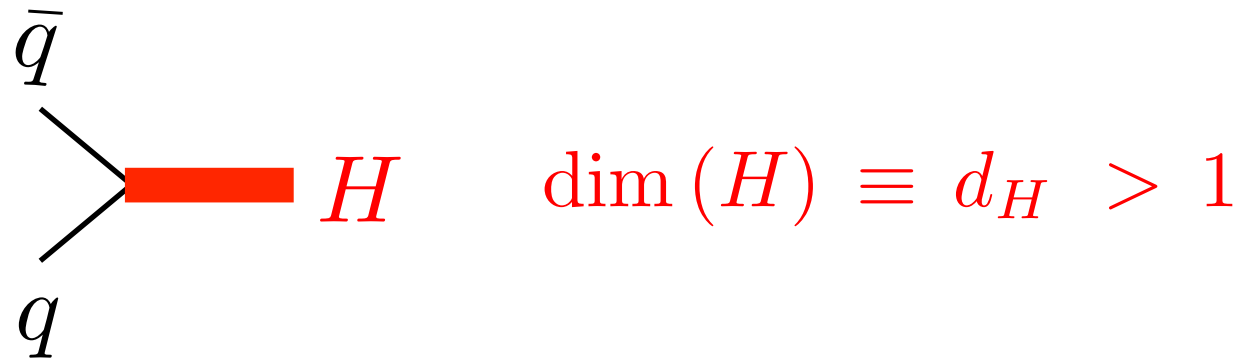
....

Huber

RS with bulk fermions



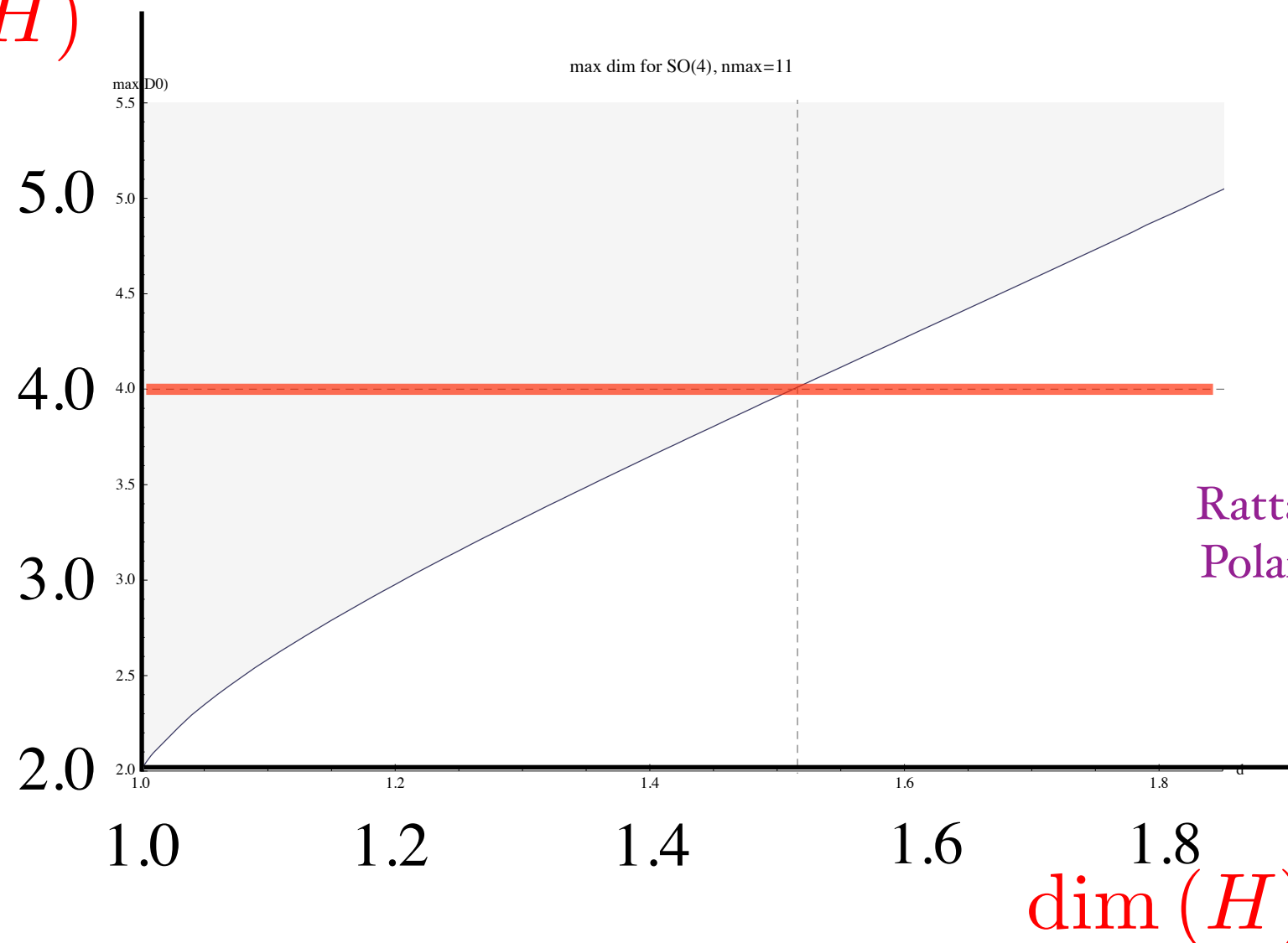
Yukawas are *irrelevants*
 m_t hard to produce



$$\dim(\bar{q}qH) = 4 + (d_H - 1) > 4$$

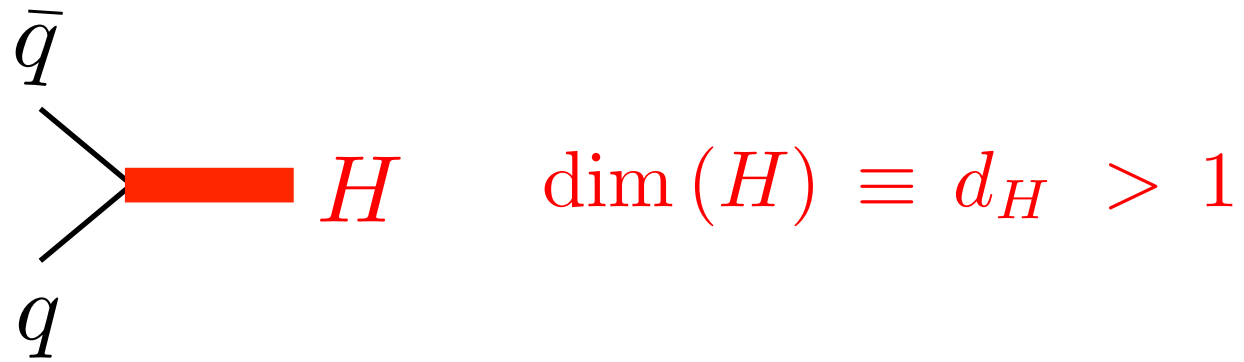
question: how close can I push $d_H \rightarrow 1$
 without getting back the hierarchy problem?

$\dim(H^\dagger H)$



Rattazzi, Rychkov, Tonni, Vichi '08
 Poland, Simmons-Duffin, Vichi '11

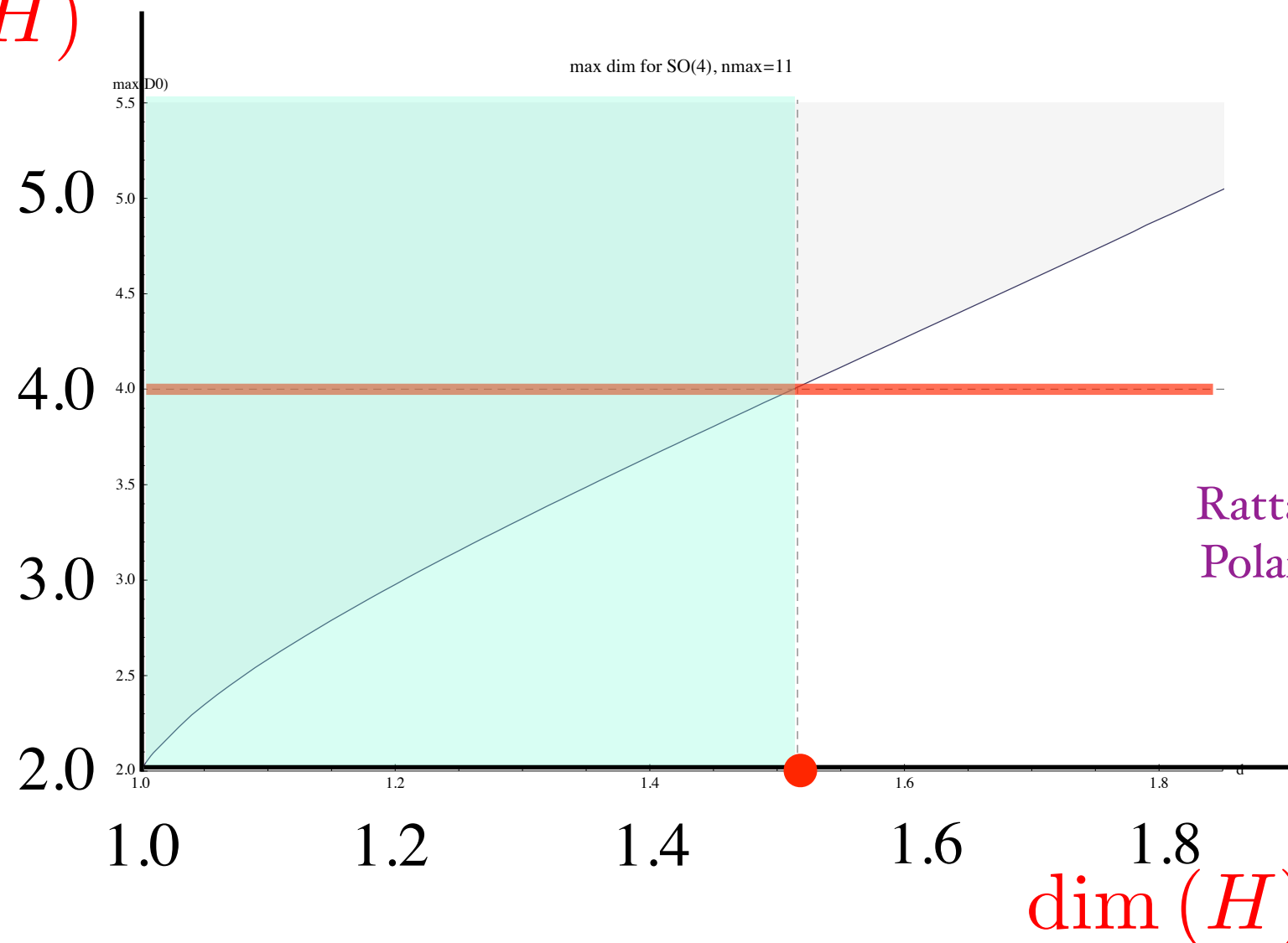
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Flavor from partial compositeness

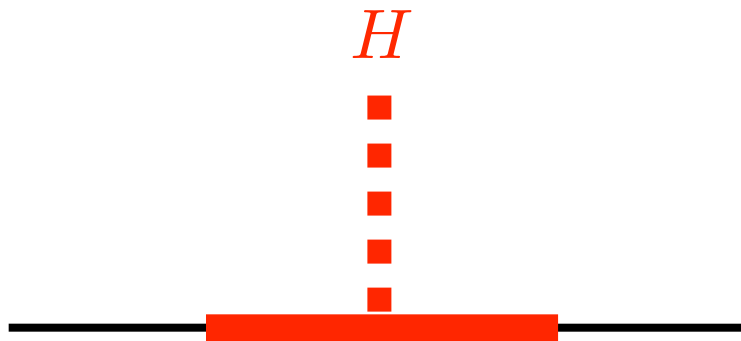
D.B. Kaplan '91

....

Huber, Shafi '00

RS with bulk fermions

$$\mathcal{L}_{Yukawa} = \epsilon_q^i q_L^i \Psi_q^i + \epsilon_u^i u_L^i \Psi_u^i + \epsilon_d^i d_L^i \Psi_d^i$$



$$Y_u^{ij} \sim \epsilon_q^i \epsilon_u^j g_*$$

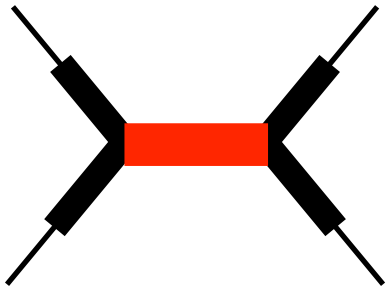
$$Y_d^{ij} \sim \epsilon_q^i \epsilon_d^j g_*$$

Ψ = composite with dimension $\sim \frac{5}{2}$  $\epsilon_q^i, \epsilon_u^i, \epsilon_d^i$ = dimensionless

- Hypothesis seems a bit wishful to me, but I see no other option
- Problems of minimal technicolor greatly alleviated, but not eliminated

Flavor transitions controlled by selection rules

$\Delta F=2$



$$\epsilon_q^i \epsilon_d^j \epsilon_q^k \epsilon_d^\ell \times \frac{g_\rho^2}{m_\rho^2} (\bar{q}^i \gamma^\mu d^j)(\bar{q}^l \gamma_\mu d^\ell)$$

$\Delta F=1$



$$\epsilon_q^i \epsilon_u^j g_\rho \times \frac{v}{m_\rho^2} \times \frac{g_\rho^2}{16\pi^2} \bar{q}^i \sigma_{\mu\nu} u^j G_{\mu\nu}$$

Bounds & an intriguing hint

Davidson, Isidori, Uhlig '07
Csaki, Falkowski, Weiler '08

Keren-Zur, Lodone, Nardecchia, Pappadopulo, RR, Vecchi '12

ϵ_k	$m_\rho \gtrsim 10 \text{ TeV}$
$\epsilon'/\epsilon, \quad b \rightarrow s\gamma$	$m_\rho \gtrsim \frac{g_\rho}{4\pi} \times (10 - 15) \text{ TeV}$
d_n	$m_\rho \gtrsim \frac{g_\rho}{4\pi} \times (20 - 40) \text{ TeV}$
CP violation in D decays $\Delta a_{CP} = a_{KK} - a_{\pi\pi} = -(0.67 \pm 0.16)\%$	$m_\rho \simeq \frac{g_\rho}{4\pi} \times 10 \text{ TeV}$

- connection with weak scale not perfect
- Not crazy at all to see deviation in D's first !
- d_n should be next

tuning

$$0.1\% \left(\frac{m_h}{125 \text{ GeV}} \right)^2 \left(\frac{10 \text{ TeV}}{m_\rho} \right)^2$$

$$\mu \rightarrow e\gamma$$

$$\frac{\sqrt{m_\mu m_e}}{m_\rho^2} \bar{\mu} \sigma_{\alpha\beta} e F^{\alpha\beta}$$

MEG: $\text{Br}(\mu \rightarrow e \gamma) < 2.4 \times 10^{-12}$

$$m_\rho \gtrsim 150 \text{ TeV}$$

Partial compositeness clearly cannot be the full story

Must assume strong sector possesses some flavor symmetry

Range of
possibilities



$$U(1)_e \times U(1)_\mu \times (1)_\tau$$

...

$$SU(3) \times SU(3) \times \dots$$

Redi, Weiler '11
Barbieri et al. '12

Higgs potential, fine-tuning and expectations at the LHC

Higgs's mass versus top-partners'

$$V(h) = \begin{array}{c} t_L \\ \text{---}\circ\text{---} \\ T \\ O(\lambda_L^2) \end{array} + \begin{array}{c} t_R \\ \text{---}\circ\text{---} \\ T \\ O(\lambda_R^2) \end{array} + \dots$$

$$\lambda_L \lambda_R \sim \lambda_t g_T$$

best option

t_R is fully composite $\text{SO}(5)$ singlet

$$\lambda_L \sim \lambda_t$$

$$\lambda_R \sim g_T$$

$$V(h) = \frac{m_T^4}{g_T^2} \times \frac{\lambda_t^2}{16\pi^2} \times F(h/f)$$

Higgs's mass versus top-partners'

$$V(h) = \text{[Diagram: Loop with } t_L \text{ and red arc } T \text{]} + \text{[Diagram: Loop with } t_R \text{ and red arc } T \text{, crossed out with a green X]} + \dots$$

$O(\lambda_L^2)$ $O(\lambda_R^2)$

$$\lambda_L \lambda_R \sim \lambda_t g_T$$

best option

t_R is fully composite SO(5) singlet

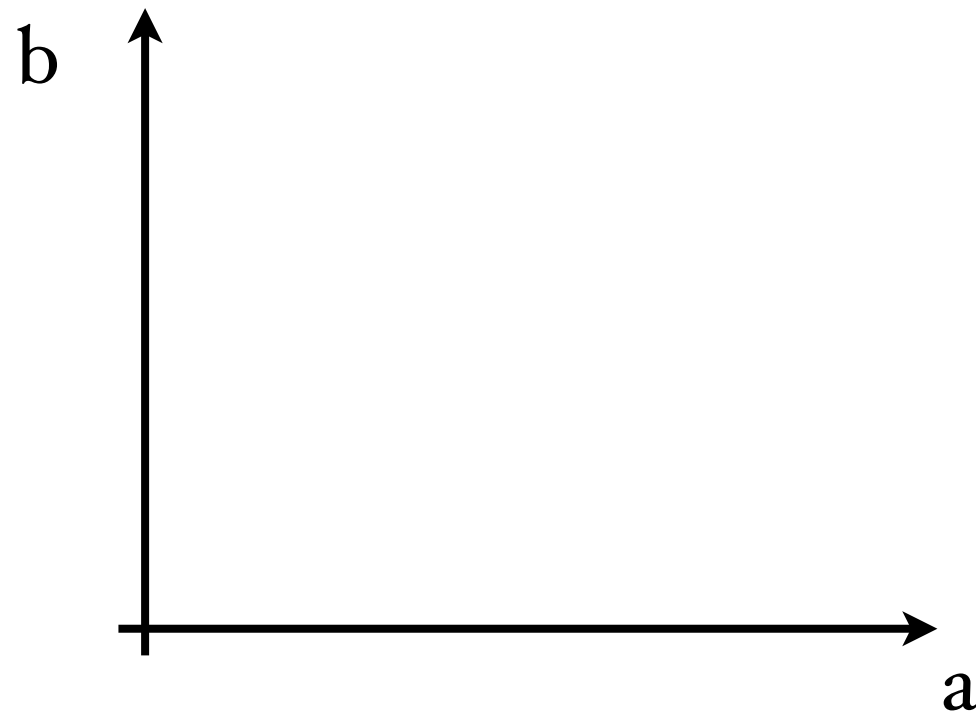
$$\lambda_L \sim \lambda_t$$

$$\lambda_R \sim g_T$$

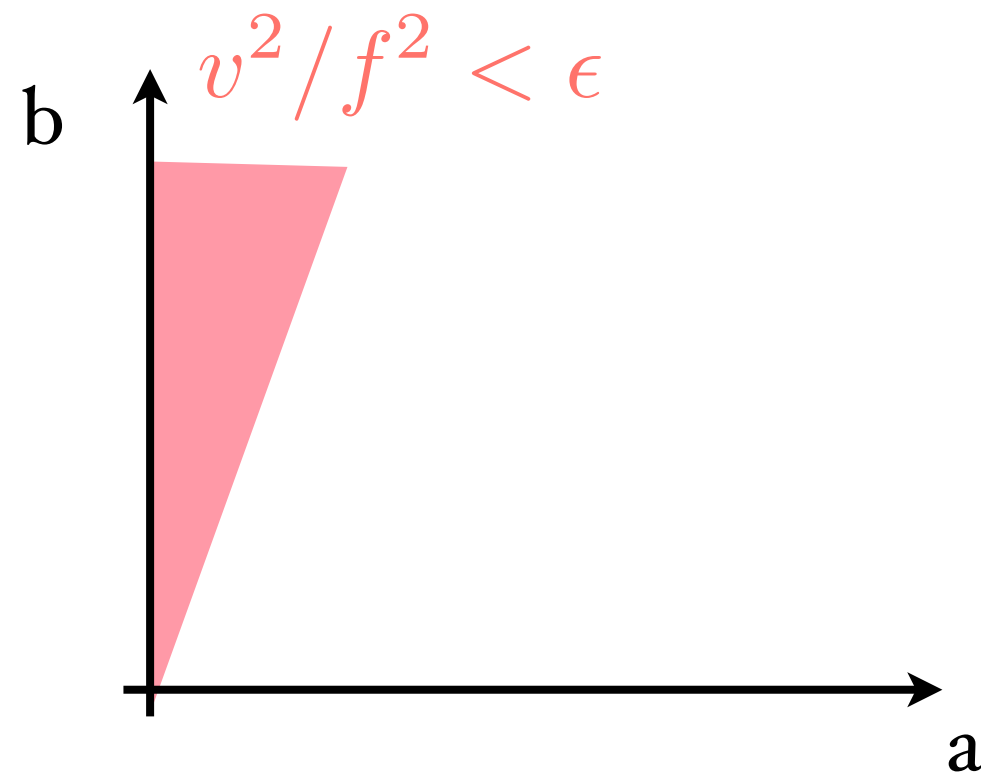
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Mrazek et al, '11
Pomarol, Riva '12

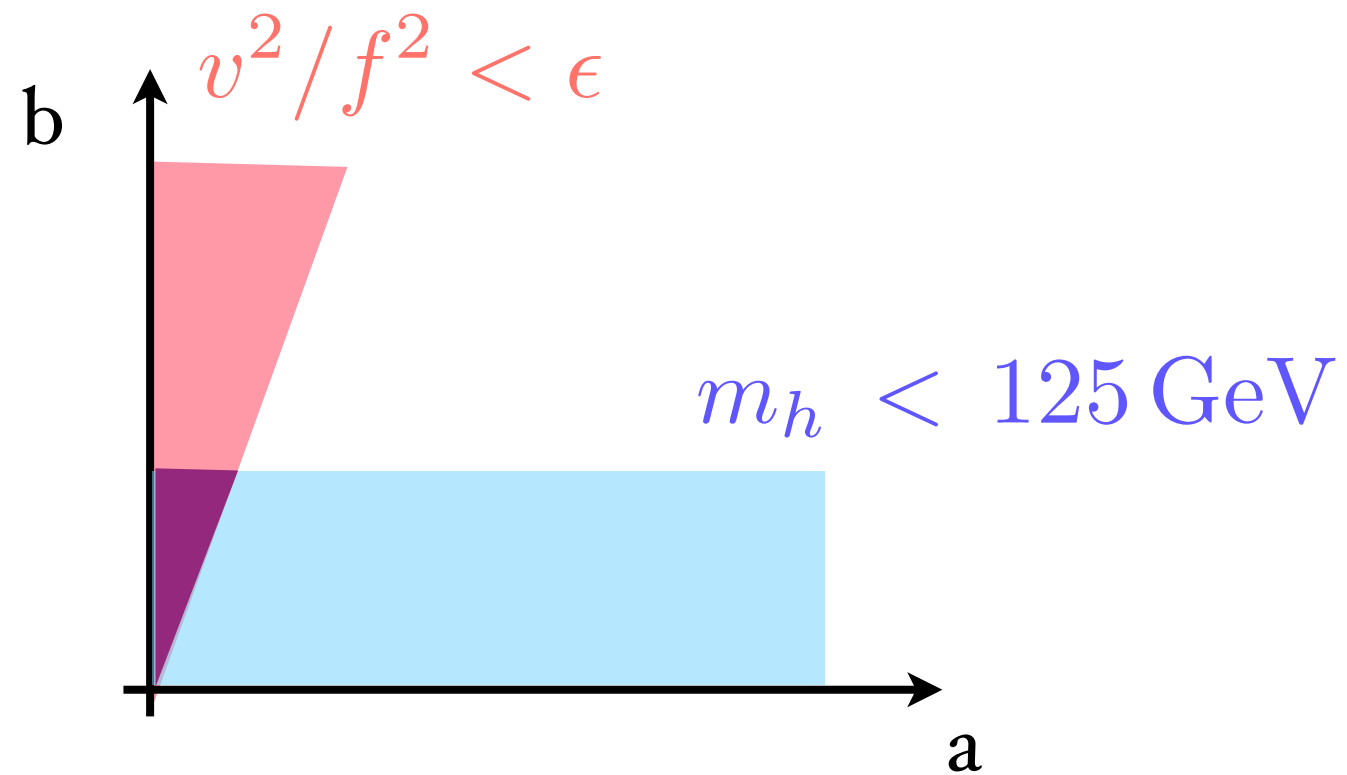
$$V = \frac{3\lambda_t^2 m_T^2}{16\pi^2} (ah^2 + bh^4/f^2 + \dots)$$



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$$\text{Total tuning} \sim \text{area} = \left(\frac{430 \text{ GeV}}{m_T} \right)^2 \times \frac{4}{g_T^2}$$

The main test of naturalness is the search for fermionic top partners

Perelstein, Pierce, Peskin '03
Contino, Servant '08
Mrazek, Wulzer '10

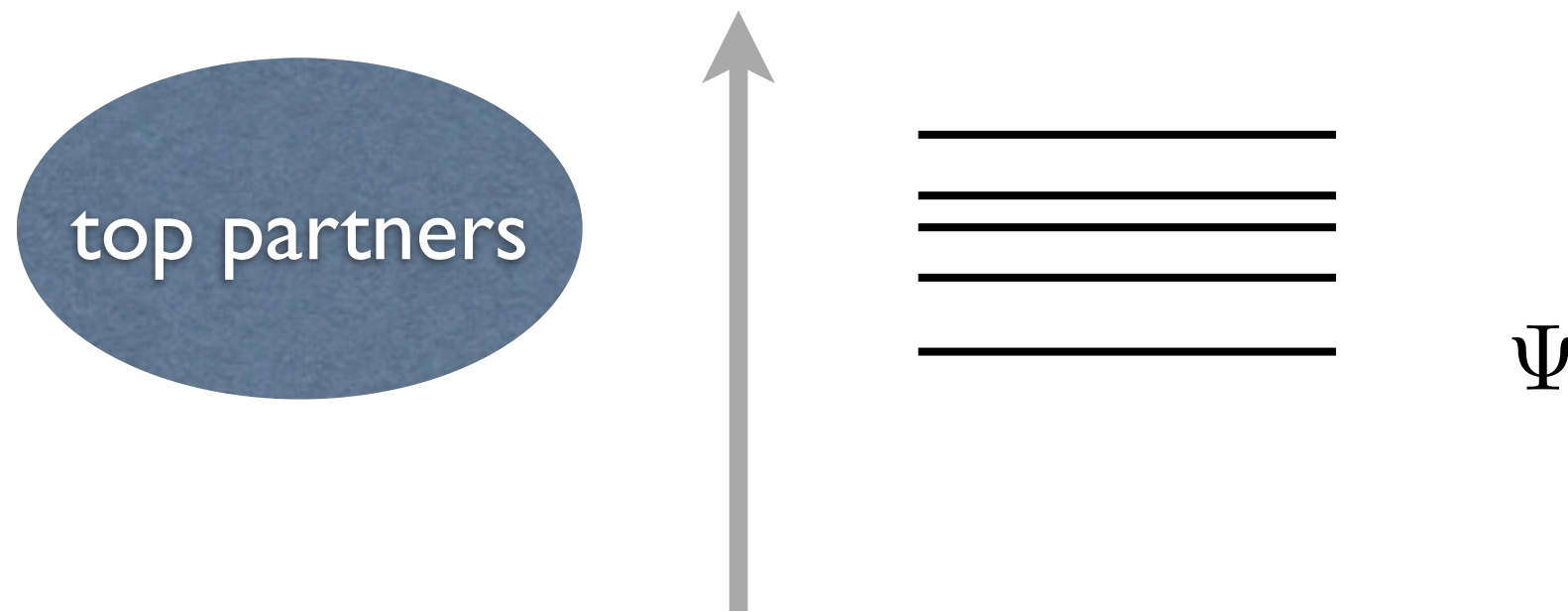
but how to proceed? given we do not have in our hand
a truly compelling and calculable model

how to help our experimental colleagues to express the
results of their searches in the light of more interesting
scenarios than, say, a fourth family

Simplified Model Ideology

in the end model builders mistrust full fledged models

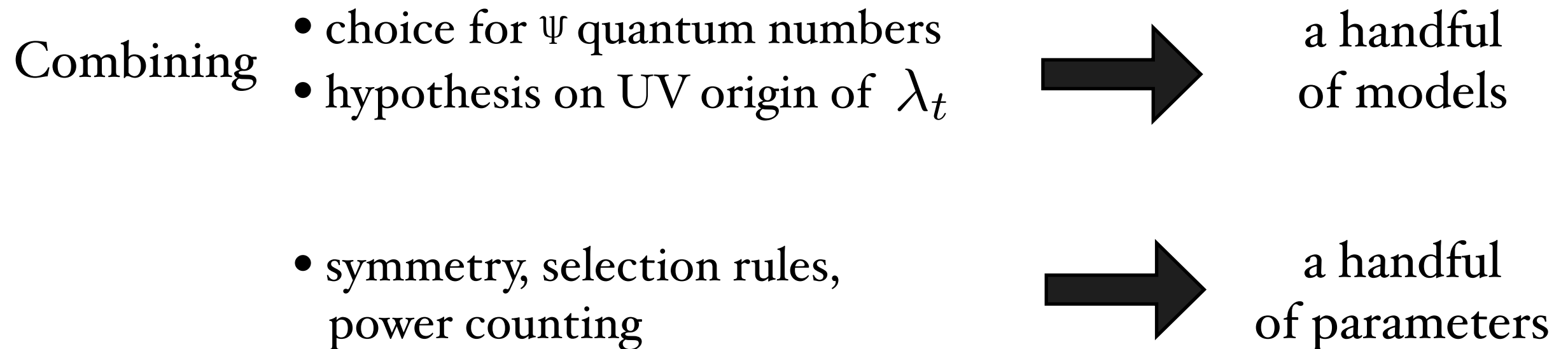
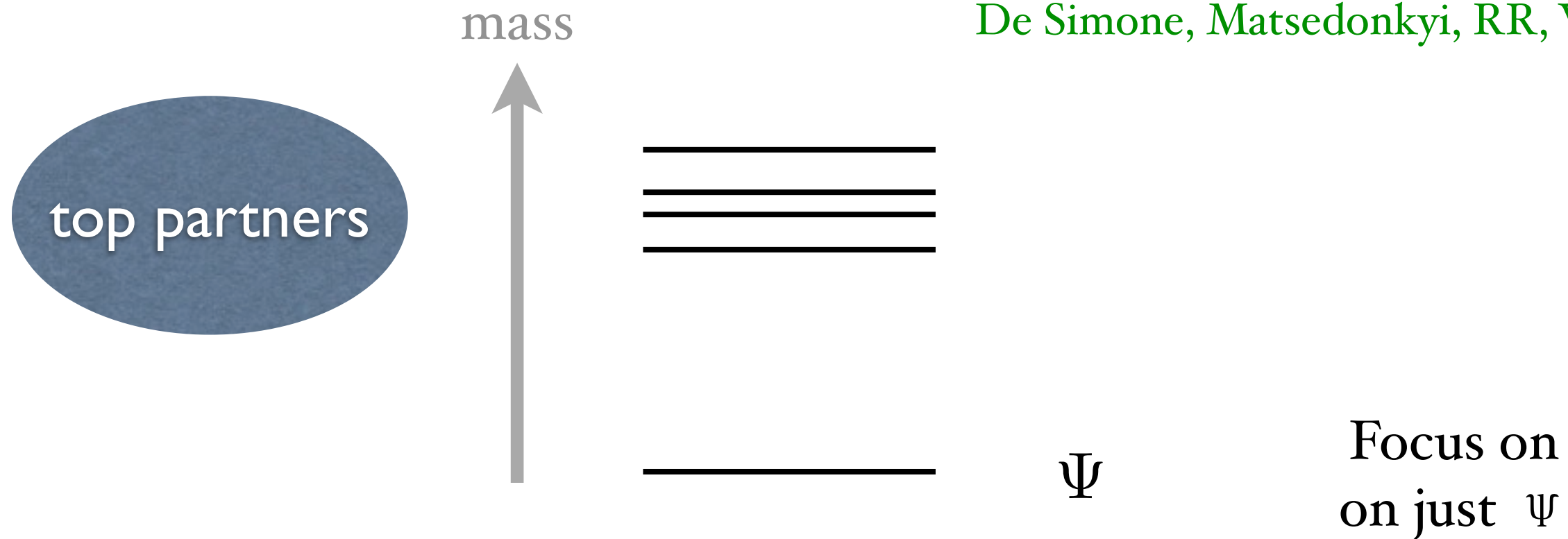
De Simone, Matsedonkyi, RR, Wulzer '12



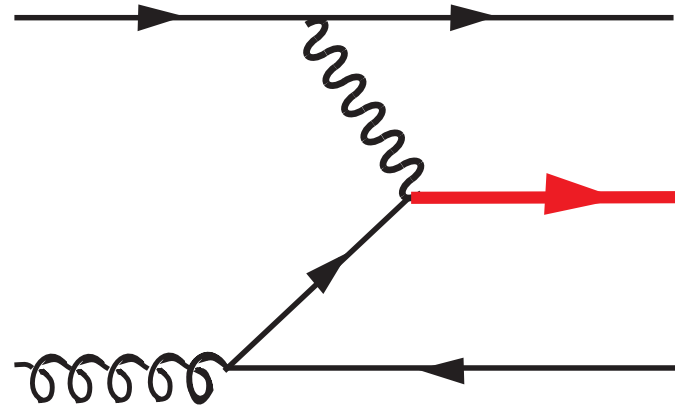
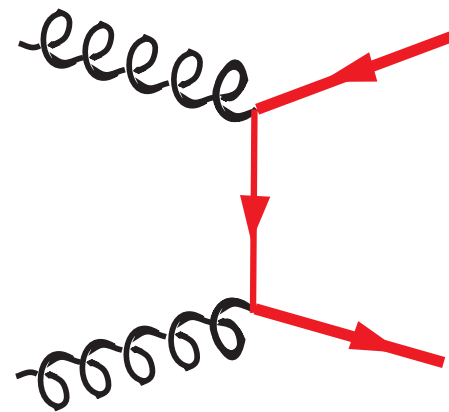
Simplified Model Ideology

in the end model builders mistrust full fledged models

De Simone, Matsedonkyi, RR, Wulzer '12

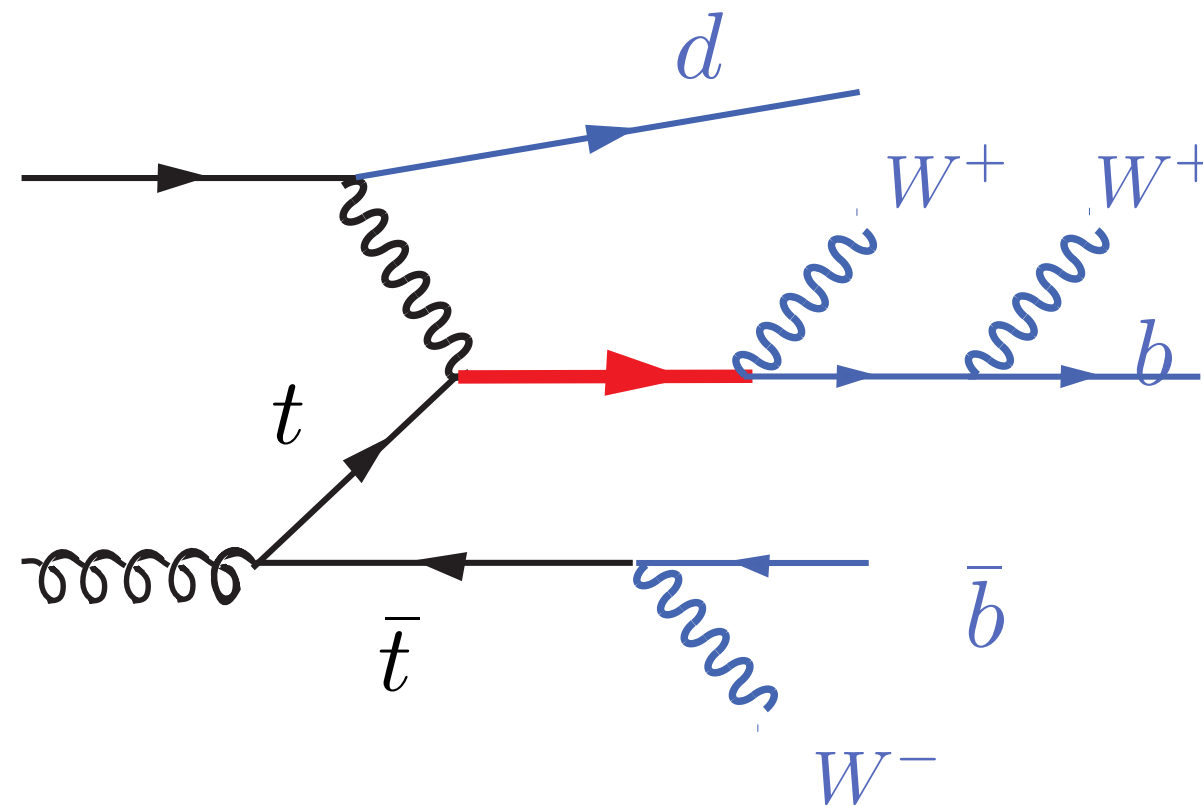


Production



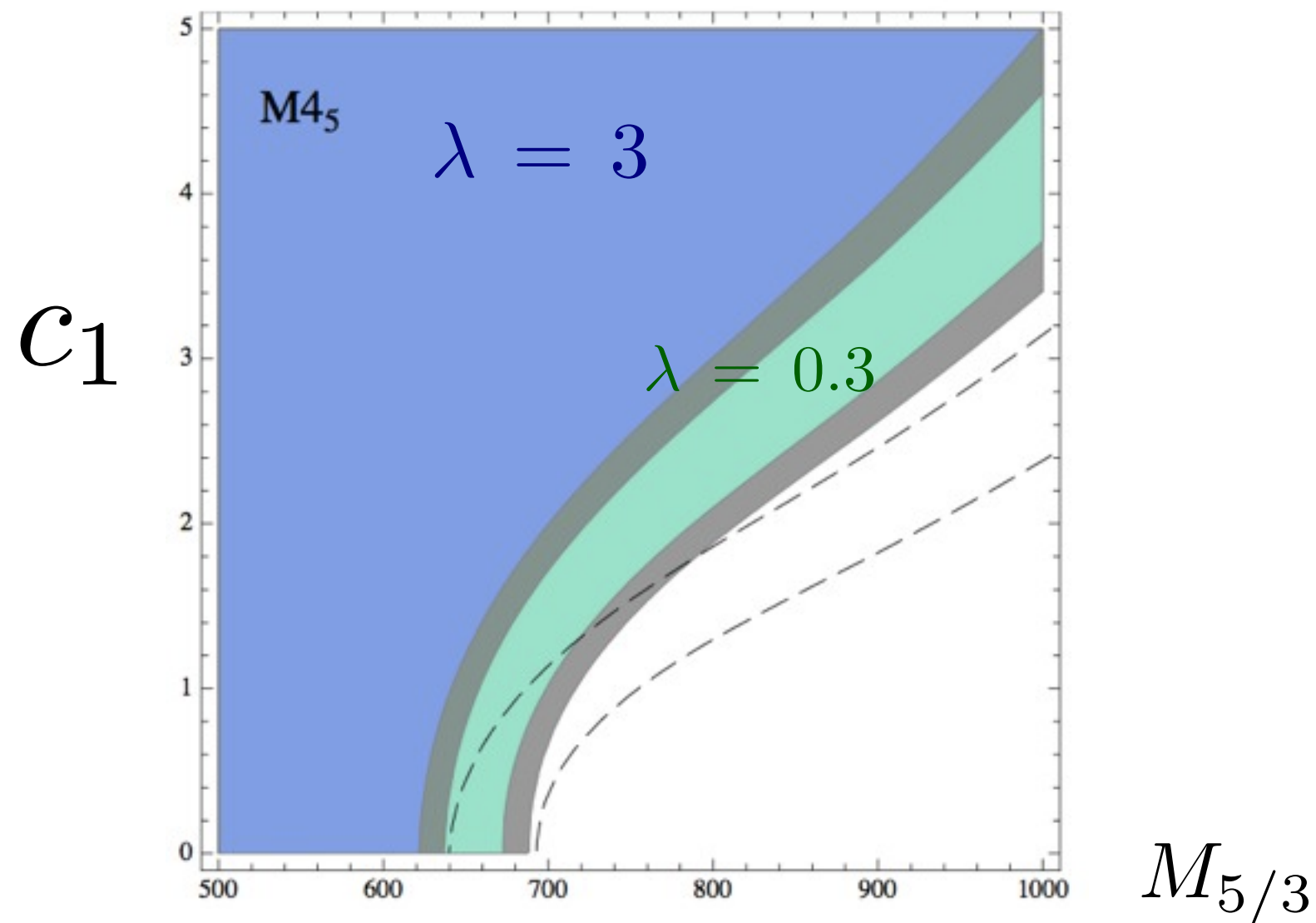
Decay

Ex.: $\Psi_{5/3} \in \left(\frac{1}{2}, \frac{1}{2}\right)$



Contino, Servant 2008

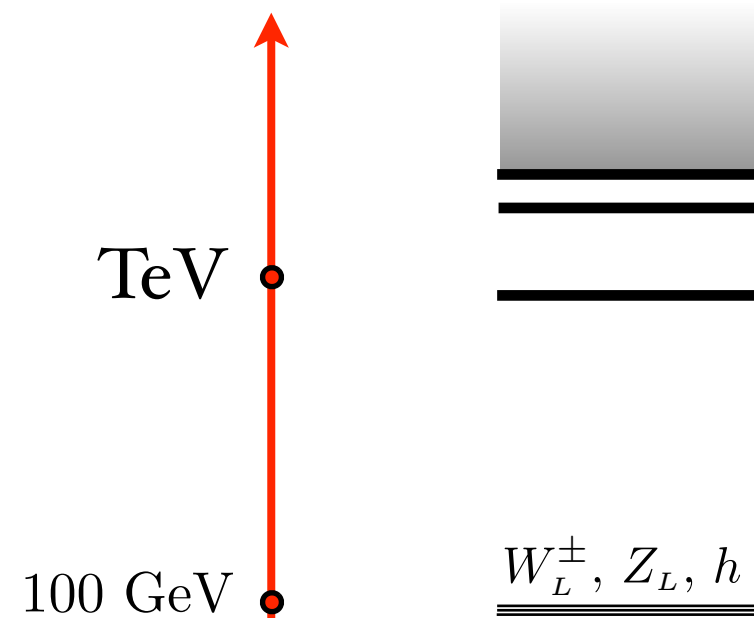
$\Psi_{5/3}$ et $\Psi_{-1/3} \in (\frac{1}{2}, \frac{1}{2})$ constrained by 4th family search $b' \rightarrow Wt$
 same sign dileptons (trileptons) + b + 3 (2) jets



$$\xi \equiv \frac{v^2}{f^2} = 0.2$$

At 14 TeV with ab^{-1} , one expects a reach of up to 2 TeV mass

Mrazek, Wulzer '10

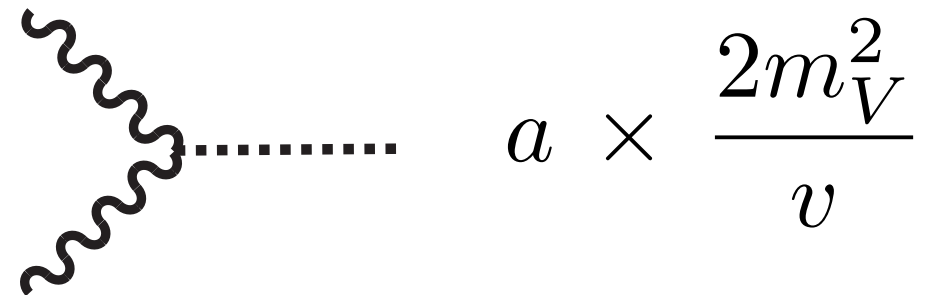


Effective Lagrangian for a composite light Higgs boson (+ pseudo-Goldstone hypothesis)

Giudice, Grojean, Pomarol, RR, 2007

Two leading operators in effective lagrangian

$$\# \frac{1}{2f^2} \partial_\mu |H|^2 \partial^\mu |H|^2$$

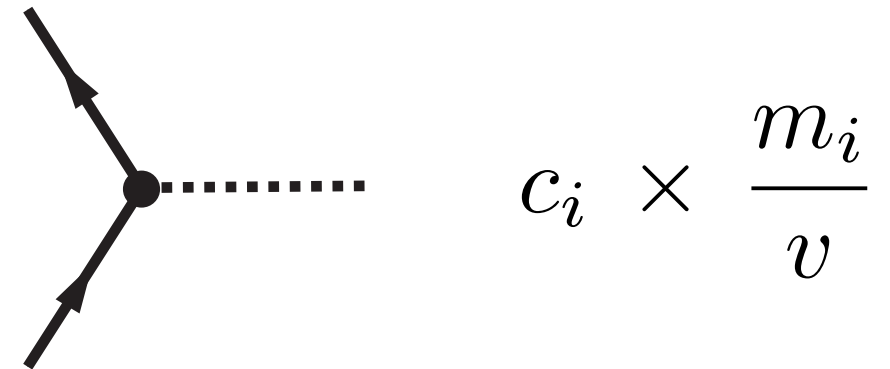


$$a \times \frac{2m_V^2}{v}$$

$$a \simeq 1 - \frac{1}{2} \frac{v^2}{f^2} < 1$$

robust consequence
of coset structure

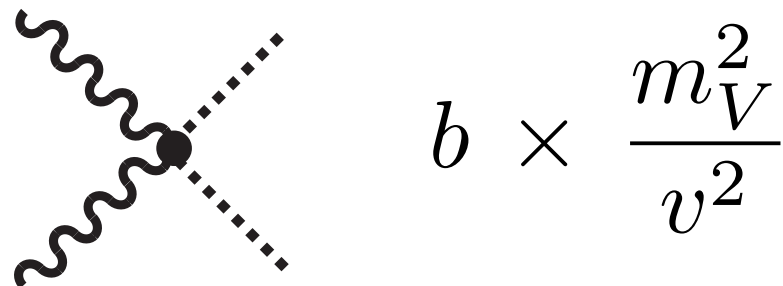
$$\# \frac{y_i}{f^2} (\bar{f}_i f_i H) |H|^2$$



$$c_i \times \frac{m_i}{v}$$

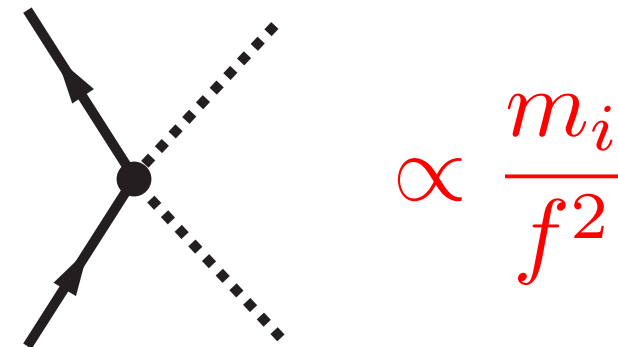
$$c_i \simeq 1 + O\left(\frac{v^2}{f^2}\right) < 1$$

generic but not a theorem



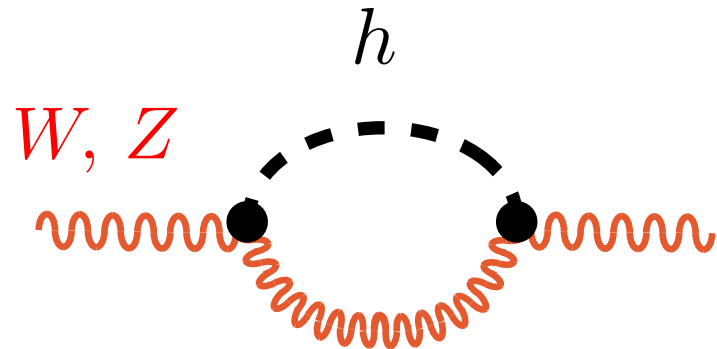
$$b \times \frac{m_V^2}{v^2}$$

$$b \simeq 1 - 2 \frac{v^2}{f^2}$$



$$\propto \frac{m_i}{f^2}$$

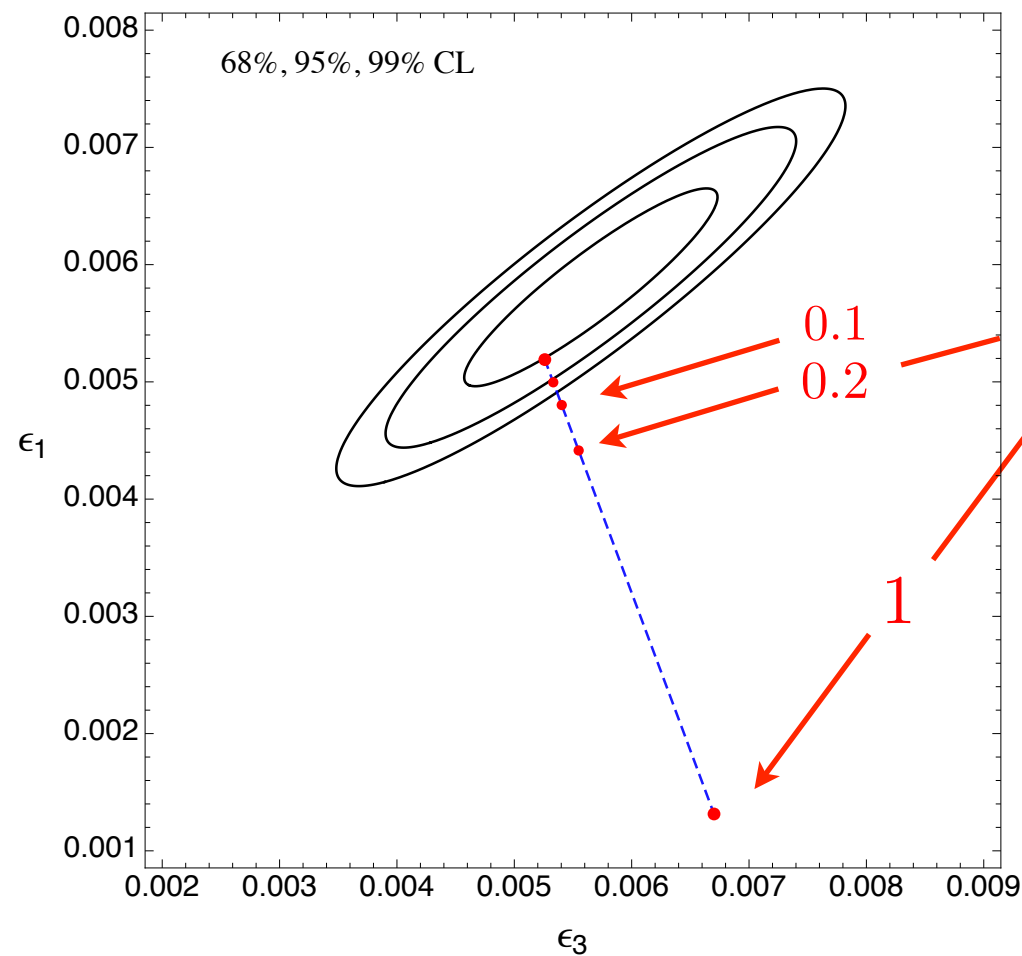
New!



$$(T) \quad \Delta\epsilon_1 = -\frac{3g^2 \tan^2 \theta_W}{32\pi^2} (1 - a^2) \ln(m_\rho/m_h)$$

$$(S) \quad \Delta\epsilon_3 = \frac{g^2}{96\pi^2} (1 - a^2) \ln(m_\rho/m_h)$$

Barbieri, Bellazzini, Rychkov, Varagnolo 07

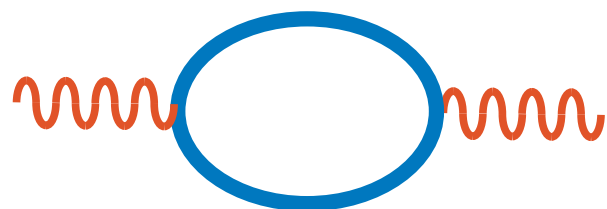


$$\frac{v^2}{f^2} = 1 - a^2$$

$$\frac{v^2}{f^2} \sim 0.1 \div 0.2$$

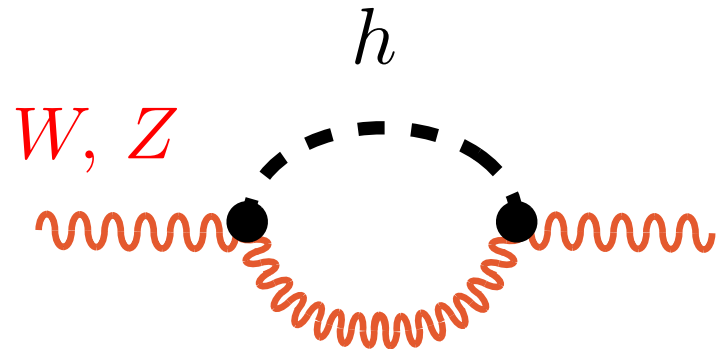
is tolerable

top-partner
loops



$$\Delta\epsilon_1 \gtrsim 10^{-3}$$

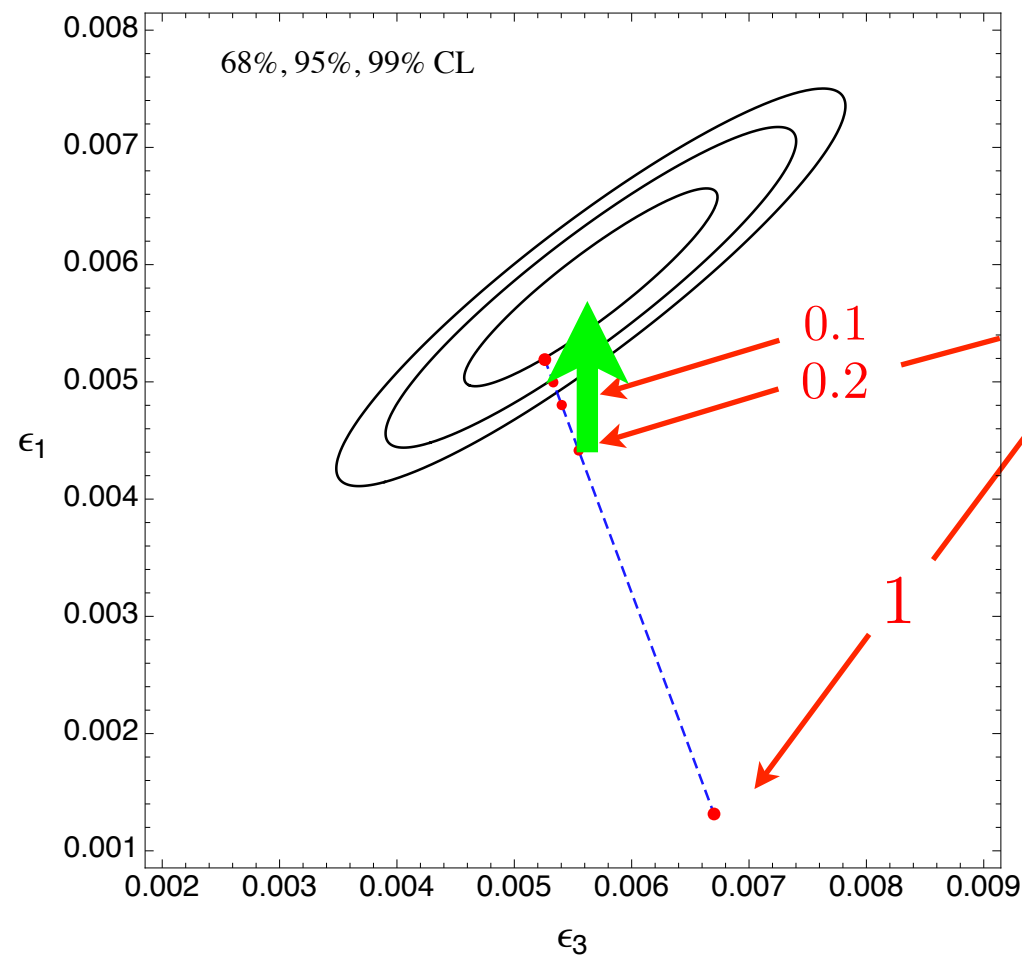
$$M_\Psi < 1 \text{ TeV}$$



$$(T) \quad \Delta\epsilon_1 = -\frac{3g^2 \tan^2 \theta_W}{32\pi^2} (1 - a^2) \ln(m_\rho/m_h)$$

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Barbieri, Bellazzini, Rychkov, Varagnolo 07

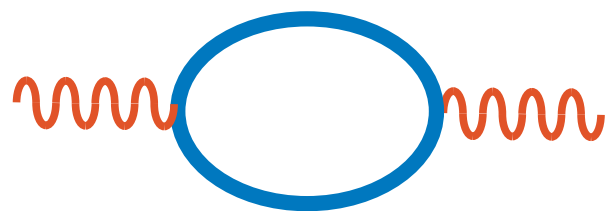


$$\frac{v^2}{f^2} = 1 - a^2$$

$$\frac{v^2}{f^2} \sim 0.1 \div 0.2$$

is tolerable

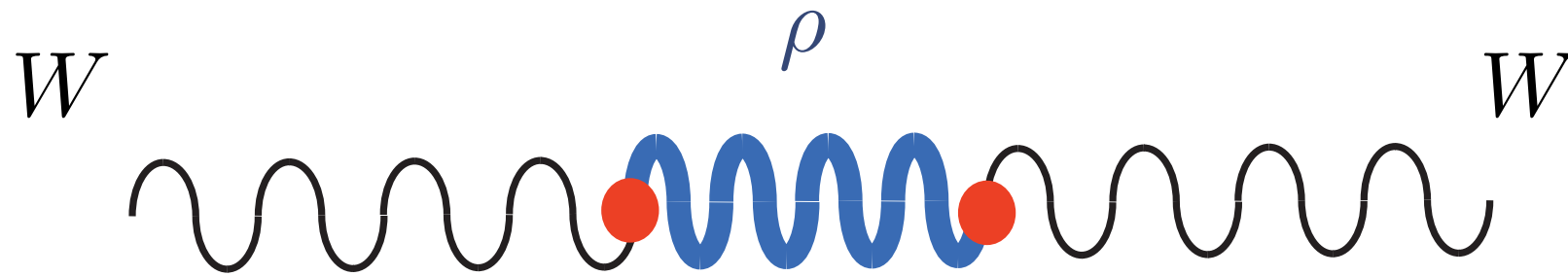
top-partner
loops



$$\Delta\epsilon_1 \gtrsim 10^{-3}$$

$$M_\Psi < 1 \text{ TeV}$$

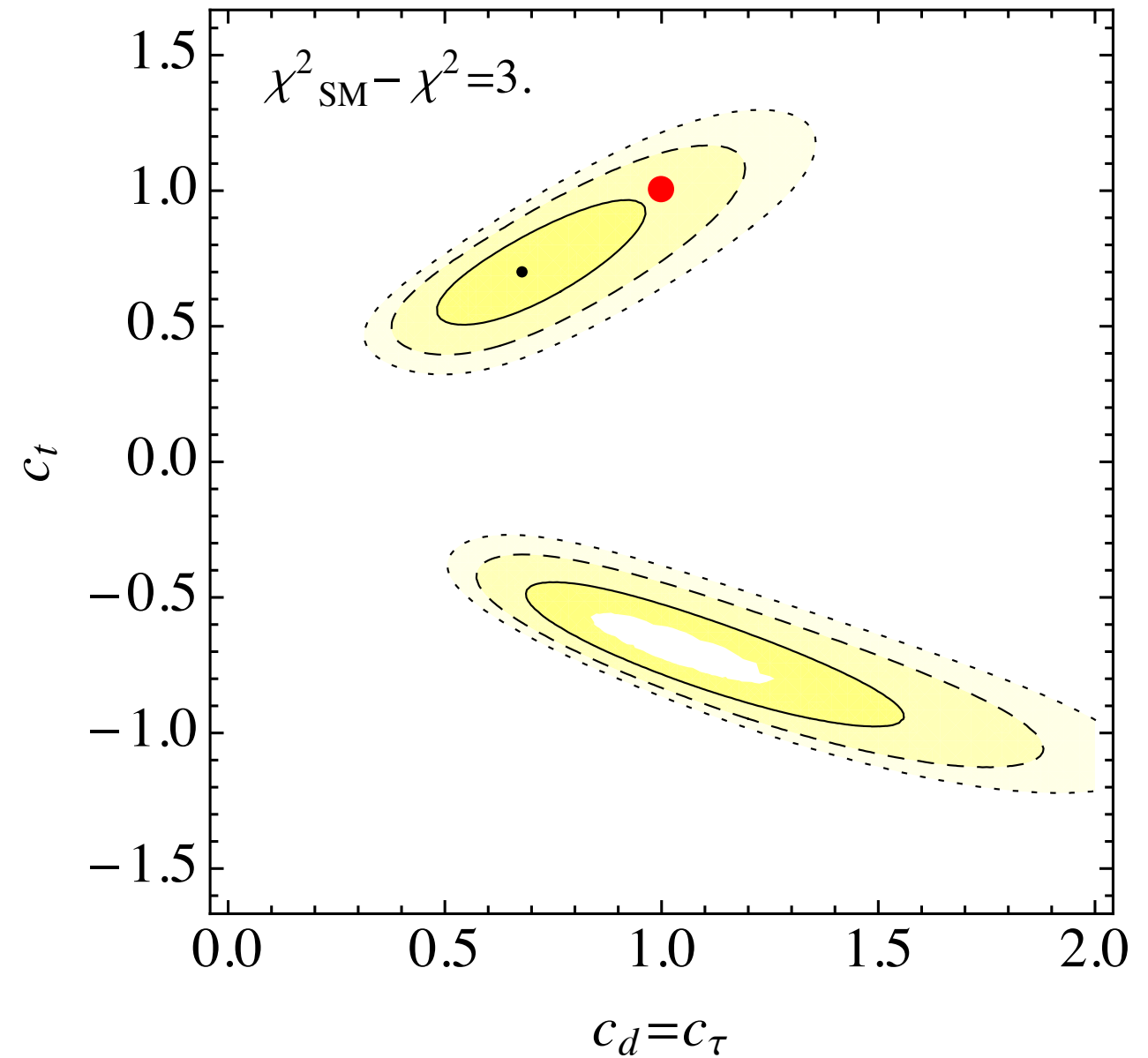
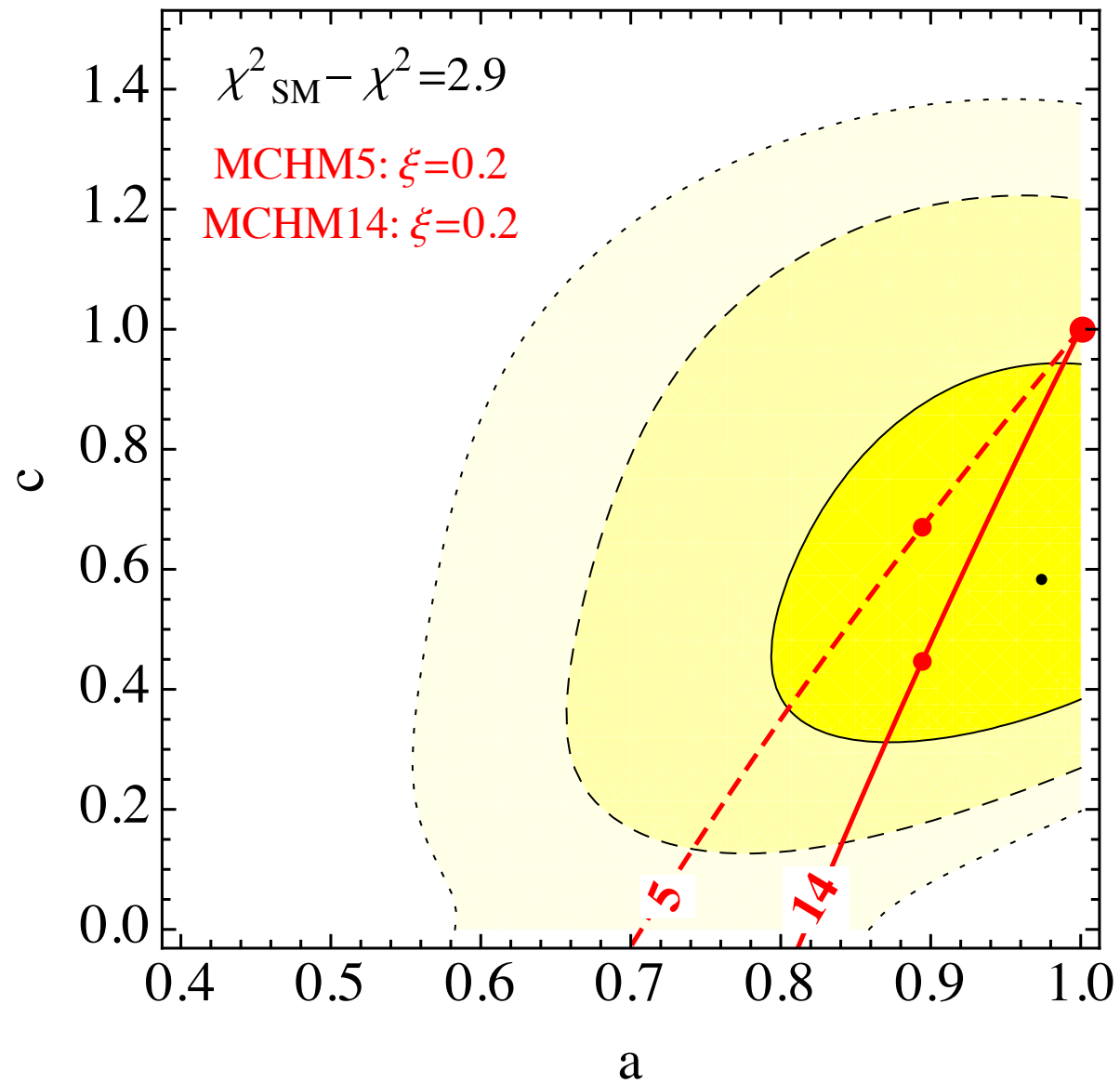
vector resonances



$$\Delta\epsilon_3 \sim \frac{m_W^2}{m_\rho^2}$$

$$\Delta\epsilon_3 < 10^{-3} \qquad m_\rho > 3 \text{ TeV}$$

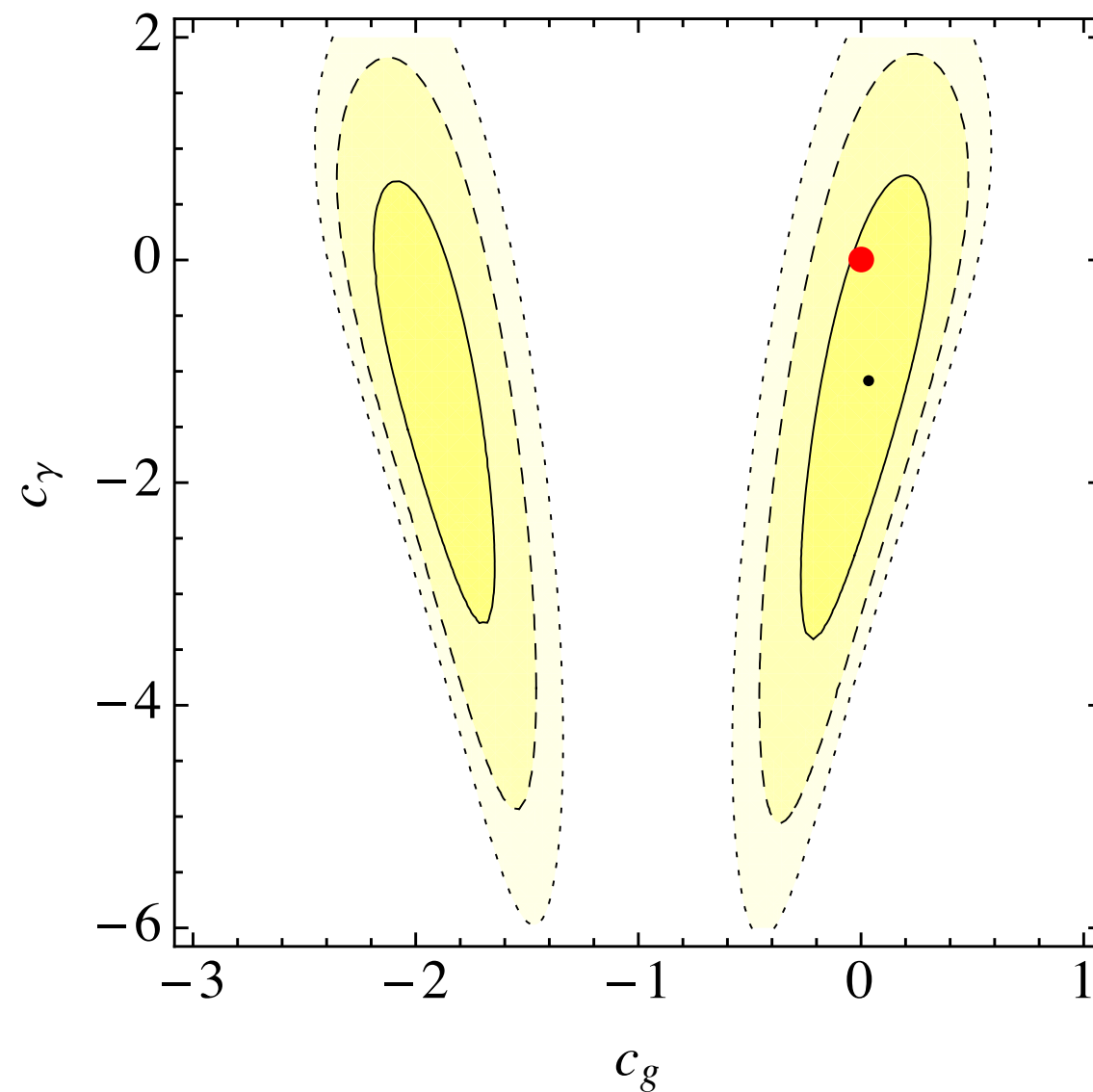
time not ripe to search for them at LHC



- overall reduction of fermion couplings is mildly favored over SM
- composite Higgs scenario not unfit
- 2HDM definitely unfit: either $c_t > 1, c_b < 1$ or $c_t < 1, c_b > 1$

Alternative lagrangian, associated with new light & weakly coupled states

$$\mathcal{L}_{eff} = c_g \frac{\alpha_s}{4\pi} \frac{h}{v} G_{\mu\nu} G^{\mu\nu} + c_\gamma \frac{\alpha}{4\pi} \frac{h}{v} F_{\mu\nu} F^{\mu\nu}$$



Future perspective on Higgs couplings

LHC 3 ab^{-1} : Single Higgs production

European Strategy Group docs
Crakow talk by Grojean

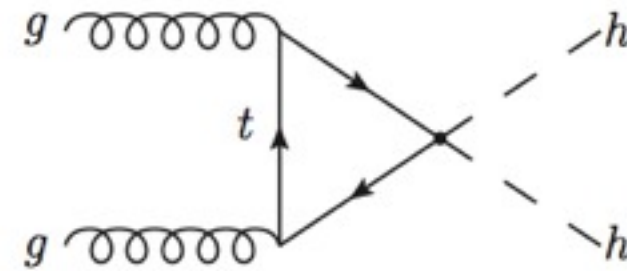
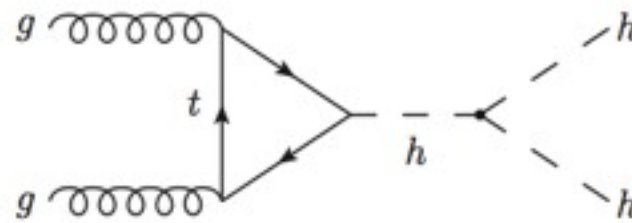
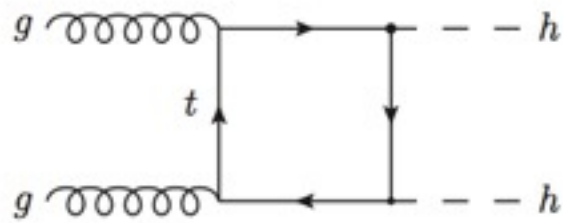
$$\Delta a = 3\%$$

$$\Delta c_f = 5\%$$

$$\frac{v^2}{f^2} \sim 0.05$$

LHC ab^{-1} : Double Higgs production

$$\frac{v^2}{f^2} \sim 0.1$$



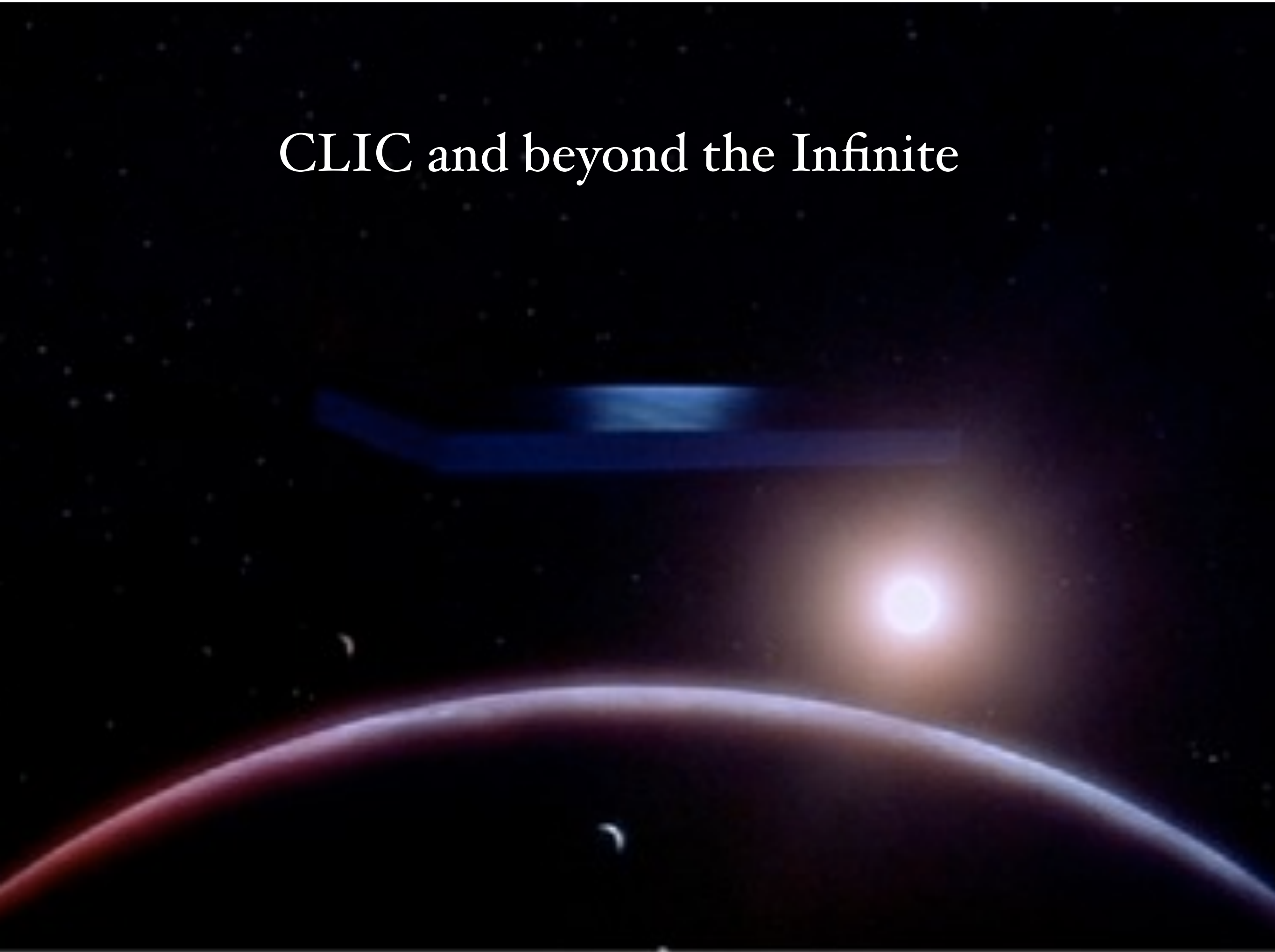
Grober, Muhlleitner 2010

Contino, Ghezzi, Moretti, Panico, Piccinini, Wulzer 2012

Linear Collider ab^{-1} : single Higgs production

$$\frac{v^2}{f^2} \sim 0.01$$

CLIC and beyond the Infinite

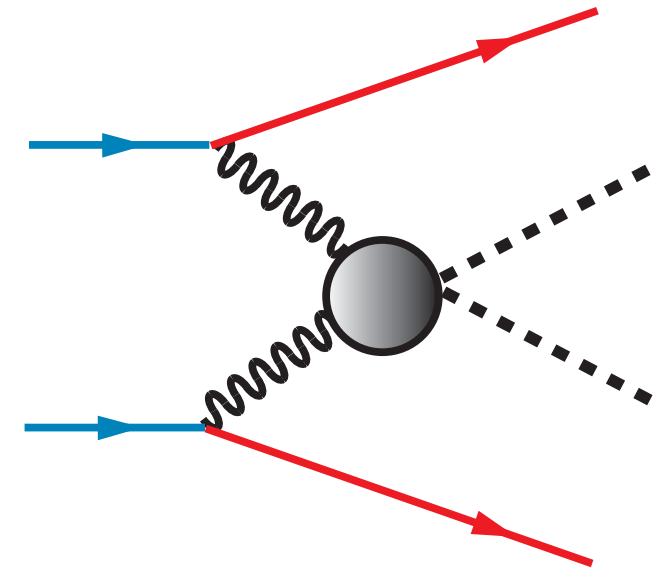


Composite h fails to fully unitarize VV scattering

$$\begin{array}{lll} \mathcal{A}(VV \rightarrow VV) = \frac{s}{v^2}(1 - a^2) & \text{Goldstone} & = \frac{s}{f^2} \\ \mathcal{A}(VV \rightarrow hh) = \frac{s}{v^2}(a^2 - b) & & = \frac{s}{f^2} \end{array}$$

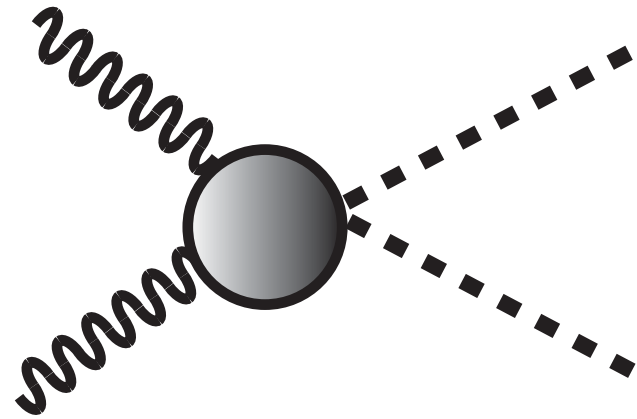
LHC ab^{-1} : sensitive to $\frac{v^2}{f^2} \gtrsim 0.3$

CLIC at 3TeV and 1 ab^{-1} : $\frac{v^2}{f^2} \gtrsim 0.01$

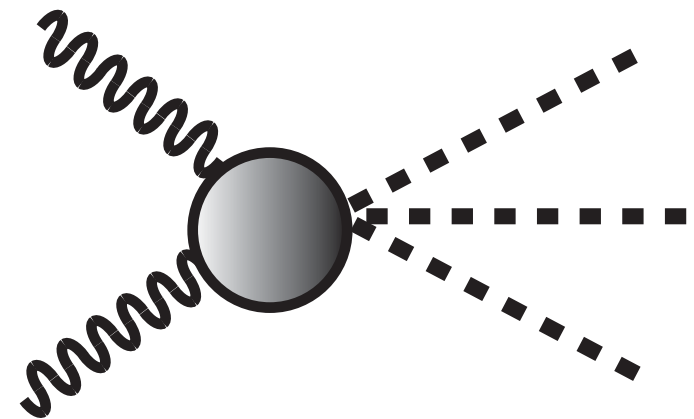


Contino, Grojean, Pappadopulo, RR, Thamm in preparation

for $\frac{v^2}{f^2} \gtrsim 0.1$ can test coset structure by considering



versus



symmetric coset
homogeneous space

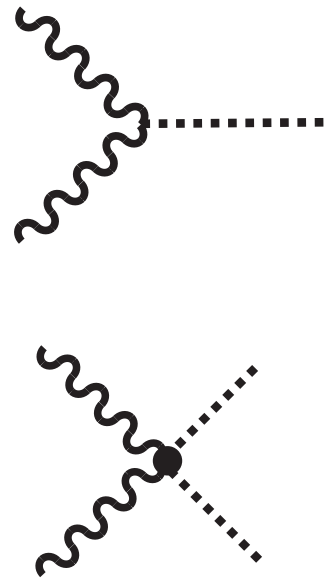
$\pi \rightarrow -\pi$ unbroken around any point

Processes with odd number of legs are suppressed

Notice: in effective lagrangian non trivial correlation of dim 6 and 8
operator coefficients

Precision versus energy frontier

indirect
and
semi-direct



sensitive to

$$\frac{1}{f^2} \sim \frac{g_\rho^2}{m_\rho^2}$$

HL-LHC

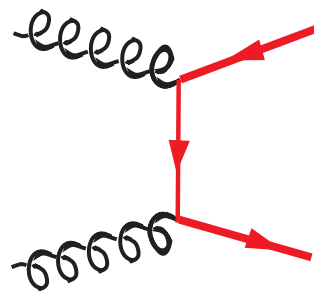
ILC

5%

1%

factor 2 in f

direct



HL-LHC

ILC

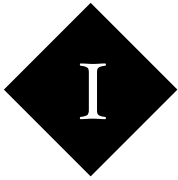
13 TeV

33TeV

factor 2 in m_ρ

The most amazing thing about the Standard Model Higgs boson

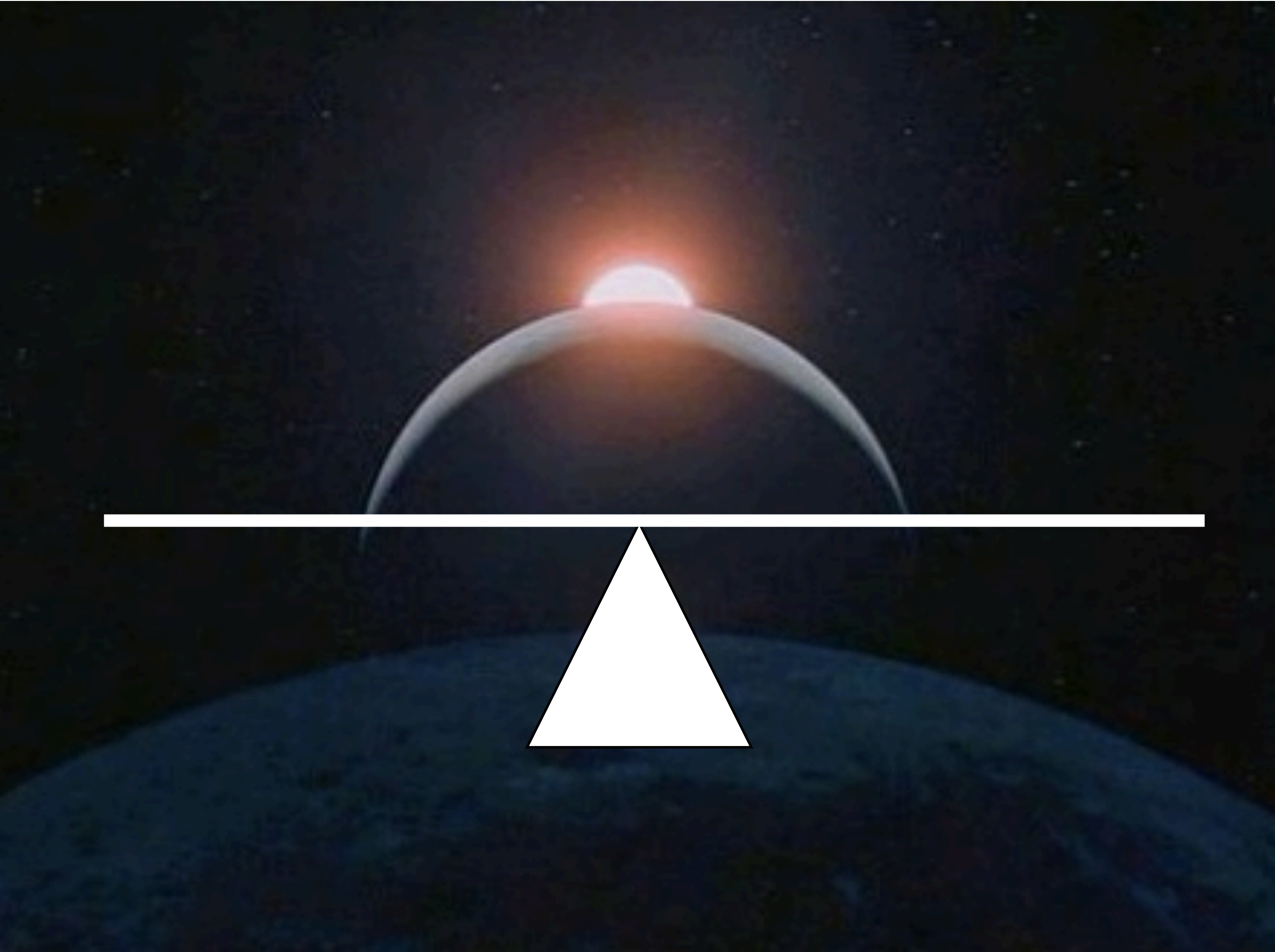
Being Elementary and Lonely

 I

- Baryon & Lepton number conservation
- Natural Flavor Conservation (CKM)
- custodial symmetry

} emergent accidents of effective theory

 II the apparent tuning of its mass parameter



Higgs mass

Yukawas

unwanted effects

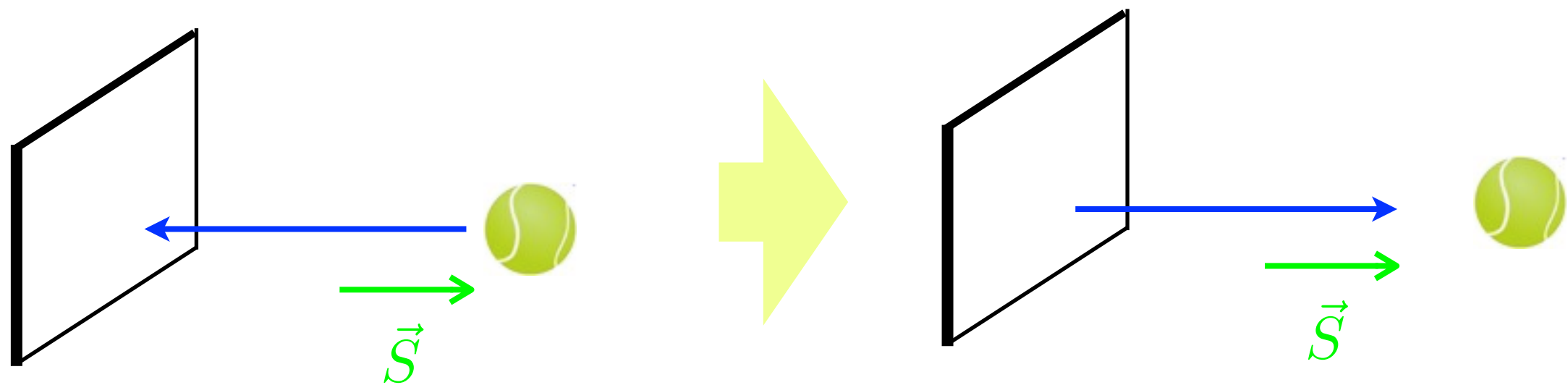


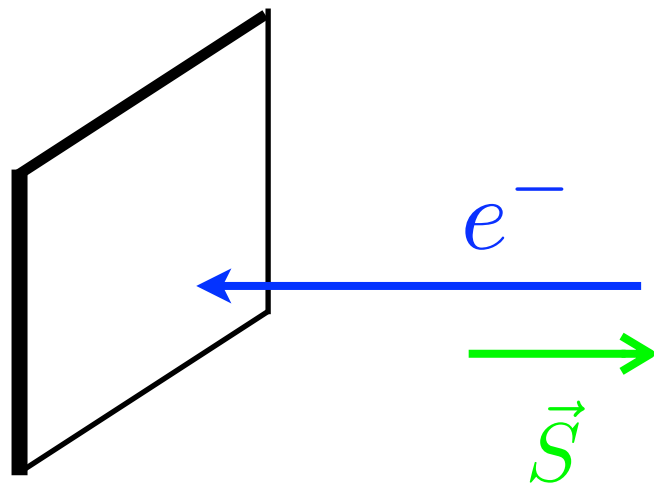
- ◆ Flavor demands a rich spectrum of composite fermion operators, with non trivial quantum numbers under color, electroweak and flavor symmetry
- ◆ In UV $\dim(\Psi) \sim 5/2$, mimicking $\dim(Hq) \simeq 5/2$ in SM
- ◆ Bosonic resonances: EW precision data want them heavy and strongly coupled. $m_\rho > 3 \text{ TeV}$ with g_ρ as big as possible
- ◆ Fermionic top partners: Naturalness wants them below 1 TeV, while $m_h = 125$ wants them more weakly coupled

If the scenario of Composite Higgs is realized in Nature it rather clear the underlying theory must be significantly more complex than a generic rescaled version of QCD !!

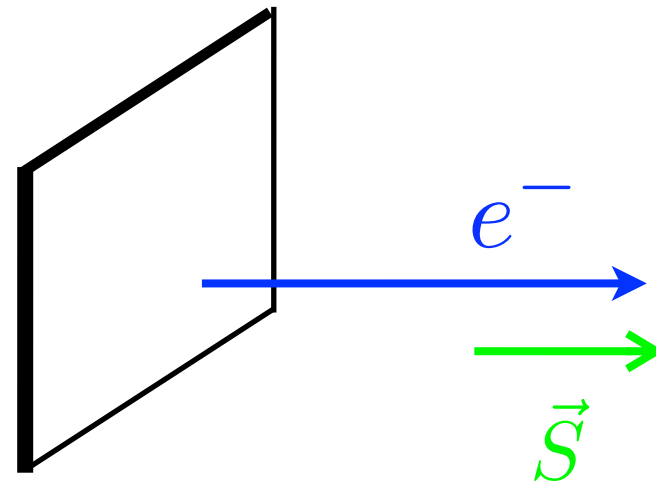
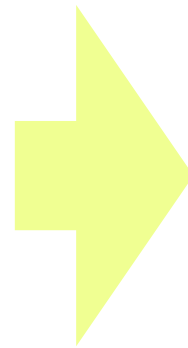
Scherzo

Gauge Invariance and Mass





e_L

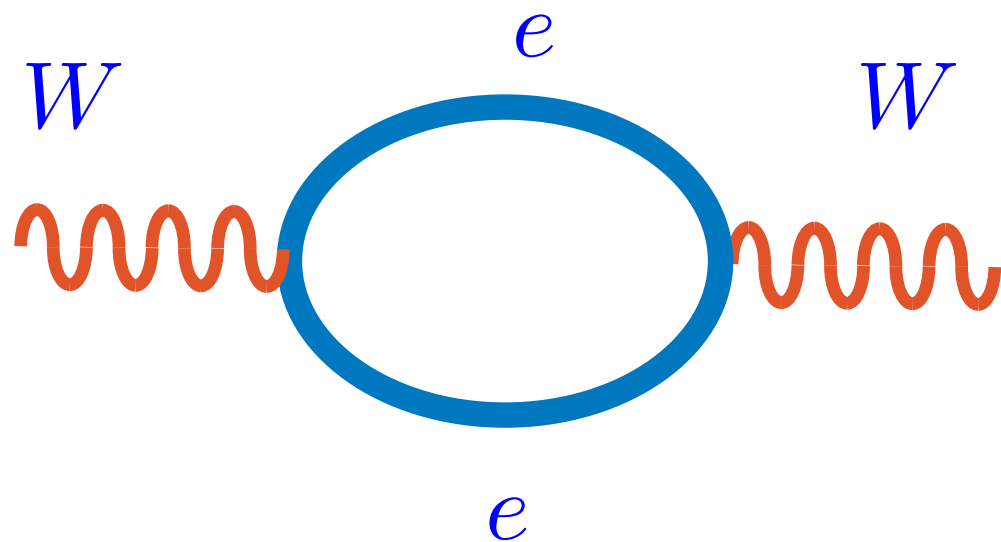
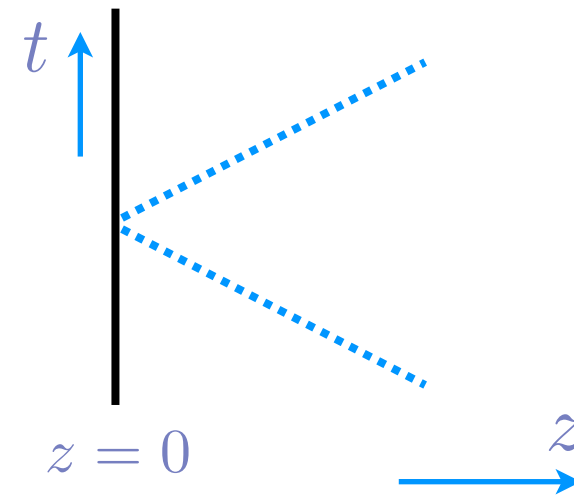


e_R

Higgsless Standard Model in AdS₄

- ❖ AdS has 2+1 *boundary* which is reached in finite coordinate time by lightlike geodesics

$$ds^2 = \frac{L^2}{z^2} (-dt^2 + dx^2 + dy^2 + dz^2)$$



$$m_W^2 \propto \frac{\alpha}{4\pi} \frac{1}{L^2}$$

Rattazzi, Redi 09

- eaten Goldstone is electron-antielectron two particle state
- theory weakly coupled
- no Higgs boson