# Studying galaxy formation with dynamical modelling

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# General framework



# Hierarchical galaxy formation



Millennium (Springel et al. 2005)





#### (Schawinski+14)





Early-type galaxy = ETG



- **Bimodal galaxy colour distribution**  $\bigcirc$
- Mergers of blue galaxies  $\rightarrow$  Red galaxies
- Feedback required for quick transition: Blue  $\rightarrow$  Red  $\bigcirc$
- Merger of red galaxies required to reach highest masses  $\bigcirc$

## What are the observables?



Integral-field spectroscopy (IFS) (Allington-Smith 2006)
Various technical approaches
All produce a three-dimensional data-cube

# The revolution of IFS surveys





#### (Emsellem+04)

SAURON survey: deZeeuw+02 48 ETGs + 24 spirals



#### (Krajnovic+11) ATLAS<sup>3D</sup> survey: Cappellari+11 260 ETGs volume-limited http://purl.org/atlas3d

# The race to large IFS samples

#### **Gas kinematics**



Credits: R. García-Benito, F. Rosales-Ortega, E. Pérez, C.J. Walcher, S.F. Sánchez & the CALIFA team (2014)

CALIFA survey: Sánchez+12 600 ETG + spiral galaxies planned, 200 in DR2 http://califaserv.caha.es/



- Multiplexed surveys:
- SAMI 13 IFUs: Bryan+15
  - 3,400 galaxies planned
- MaNGA 17 IFUs: Bundy+15
  - 10,000 galaxies planned
- Hector: Bland-Hawthorn+15
  - 100,000 galaxies planned
  - Aims for end of the decade

# Galaxy kinematics from data cubes



Galaxy image gives 0<sup>th</sup> velocity moment →Σ
 Each spectrum in data cube is Doppler shifted
 Spectrum shift gives 1<sup>st</sup> velocity moment → V
 Lines broadening gives 2<sup>nd</sup> moment → σ ...

# Dynamical modelling techniques

## Main dynamical methods

- Orbit-superposition (Schwarzschild 1979)
  - Spherical: Richstone & Tremaine (1988)
  - Axisymmetric: van der Marel et al. (1998)
  - Triaxial: van den Bosch et al. (2008)
- Velocity moments (Jeans 1922)
  - Isotropic: Binney et al. (1990)
  - Anisotropic: Cappellari (2008)

Schwarzschild's (1979) method Assume steady state (Jeans theorem)  $DF = f(x, y, z, v_x, v_y, v_z) = f(I)$ Find complete set of basis functions for DF  $DF = \sum w_j F_j(I)$  Linear superposition of observables  $O_{\alpha}(x',y') = \sum G_{\alpha}[F_j(I)]$ • Key idea: basis functions  $F_i$  are stellar orbits

# Orbital superposition









Image of orbit on sky



Time





Images of model orbits





#### **Observed galaxy image & kinematics**

- Orbital set changes with gravitational potential (e.g. black hole or dark matter)
- Find the set of orbits that better fits the data



## Fit orbits to observables

With N orbits and M observables to fit
Problem to solve in the least-squares sense:

$$\begin{pmatrix} p_{1,1} & \cdots & p_{1,N} \\ \vdots & \ddots & \vdots \\ p_{M,1} & \cdots & p_{M,N} \end{pmatrix} \begin{pmatrix} w_1 \\ \vdots \\ w_N \end{pmatrix} = \begin{pmatrix} o_1 \\ \vdots \\ o_M \end{pmatrix}$$

• 
$$\min_{x} \{ \|Ax - b\| \}$$
 with  $x > 0$ 

- Is a Non-Negative Least-Squares problem
- Has a unique (possibly degenerate) minimum
- Efficient algorithms exist (NNLS or quadratic prog.)

## Intrinsic dynamical degeneracy



#### (Krajnovic+05)

- Orbital distribution is 3D  $\rightarrow$  3D data (=IFU) needed
- But even 3D data not sufficient to constrain both DF and potential (two 3D functions)
- Degeneracies are expected! See inclination above 1

## Spherical Jeans (1922) equations

- Think hydrodynamics: pressure  $\rightarrow \sigma$
- Gravity balanced by  $\sigma$  (velocity 2<sup>nd</sup> moment)
- Simplest spherical form

$$\nu \frac{GM(r)}{r^2} = \frac{d}{dr} [\nu \sigma^2(r)] \rightarrow \rho g(z) = -\frac{d}{dz} P(z)$$

- Infer v(r) from photometry  $\Sigma(R)$
- Adopt parametrization for total mass
- Calculate PSF-convolved  $\sigma_{los}(R)$
- Fit model to data

# Solving axisymmetric Jeans eq.



Focus on velocity second moments \$\langle v\_{jk}^2 \rangle\$ only
Assume shape of velocity ellipsoid (2 ratios)
Solve hydrostatic equilibrium equations
Can this simple model describe real galaxies?

- Velocity ellipsoid from Schwarzschild's models
- Nearly spherically aligned beyond 1Re
- $\sigma_R \approx \sigma_\phi$
- $\sigma_z < \sigma_R$  on equatorial plane & symmetry axis (Cappellari+07; Thomas+09)

Maximum density along line-of-sight



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- Use Multi-Gaussian fit to images (Emsellem+94; Cappellari-02)
- Efficient Jeans solution with  $\sigma_z \neq \sigma_R \neq \sigma_\phi$  (Cappellari-08)
- Just two parameters (*i*, σ<sub>z</sub>/σ<sub>R</sub>) fit shape of both V<sub>rms</sub> and V! (http://purl.org/cappellari/software)

Galaxy structure from kinematics/dynamics

# Fast kinematics very homogeneous



Kinematics encoded by <u>one</u> number β<sub>z</sub> = 1 - σ<sub>z</sub><sup>2</sup>/σ<sub>R</sub><sup>2</sup>
 Differences entirely due to bulge/disk fraction

# Fast/slow: rotation dichotomy



Fast rotators have oblate velocity ellipsoid
 Observed scatter of 7% including models errors!
 Consistent distribution for both E and SO galaxies
 Slow rotators follow different distribution



But two major classes: non-regular/regular

# What is the shape of ellipticals?



 Trivial concept
 Difficult solution
 Profound implications Side Views

## Sphere or disk?



## Key accretion processes

#### Gas accretion



(Cappellari-11 Nature) • Two main channels a) Build up by gas accretion (+ quenching) b) Build up by dry mergers • What are their relative contributions?

# **Recognizing disks using dynamics**



**Disky Elliptical** 

**S**0 (Cappellari-16 ARA&A)

- Dynamics identifies nearly face-on disks  $\bigcirc$
- Only  $\leq 2\%$  of disk can be missed  $\mathbf{O}$

# Stellar angular momentum

Cappellari-16 ARA&A

Data from: Emsellem+11 Fogarty+15



**Non-regular** 

• Fast rotator  $\rightarrow$  inclined disk galaxies

Consistent with anisotropy trend from dynamics

• Slow rotator  $\rightarrow$  weakly triaxial c/a > 0.75

## E/SO are poor proxy for kinematics



Expected trend angular momentum vs. morphology

Explained by variation in bulge fraction

• 2/3 of classic ellipticals from RC3 are fast rotators!

# Summary of galaxy structure



Cappellari+13b)

 Bulge fraction linked to quenching of star formation (see Cappellari+11b; Kauffmann+12; Bell+12; Cheung+12; Fang+12)
 Three characteristic galaxy stellar masses

(cfr. Davies+83; Faber+97; Kauffmann+03; van der Wel+09; Geha+12)

# Summary of galaxy evolution



 Two channels of galaxy formation (e.g. Khochfar+11)
 Also explains observed black hole scaling relations (e.g. Kormendy-Ho 13, Grahm-Scott13, Krajnovic+17)
 But galaxies do not follow both in sequence!

# Hierarchical morphology evolution



#### **Fast rotators**

- Generally satellites or isolated
- Quenched by environment
- Or by internal processes
- Bulge grows with quenching

### **Core slow rotators**

- Generally near halo centre
   Sink by dynamical friction
  - Mass grows by dry mergers
  - Halo quenching

# Galaxy density profiles and dark matter

# Spirals rotation from ionized gas



- Extended curves from ionized gas (Rubin-Ford70; Roberts-Whitehurst75; Rubin+80)
- Outer curves remain flat
- Limited to optical disk
- No connection to dark matter made
- Need to estimate baryonic mass



At Lowell Observatory © Bob Rubin

# **Spirals rotation from HI**



- Radio HI observations
- Extend well beyond images
- Rotation curves still flat
- "it seems relatively certain that dark material is being detected" (Faber+Gallager79 ARA&A)



# Little dark matter in ETGs centres (1R<sub>a</sub>)



Best fitting median  $f_{DM}(R_e) = 13\%$  $\bigcirc$ 

- Fully consistent with ACDM prediction  $\bigcirc$ 
  - Fixed-halo models fitted to real ATLAS<sup>3D</sup> galaxies
  - Use NFW following  $M_{200} M_{\star}$  and  $\overline{M_{200}} \overline{c_{200}}$ (Moster+10, Behroozi+10, Guo+10)

# ETGs 2-dim dynamics to 4R<sub>e</sub>



- 14 fast rotator ETGs ( $10.2 < \log M_*/M_{\odot} < 11.7$ )
- Model ATLAS<sup>3D</sup> + SLUGGS stellar kinematics
- Median coverage of 4Re (2.0-6.2R<sub>e</sub>)
- Sample dynamics where dark matter dominates

# ETG profiles are like in spirals



#### (Cappellari+15 ApJL)

- Universal <u>total</u> mass profile to  $4R_e$ :  $\rho_{tot} \propto r^{-2.2}$
- Observed rms scatter 0.11 in logarithmic slope
- Same as strong lensing studies near R<sub>e</sub>/2 (Auger+10)

# Rotation curves in spirals and ETGs



- Similar total density profiles
- Evidence for dark matter
- Slopes consistent with ACDM predictions
- Consistent with evolution spirals  $\rightarrow$  ellipticals

# Can we rule out alternative gravity?



Use Modified Newtonian Dynamics (MOND)
Try to predict observed accelerations
Predictions consistent with the data!

# **The Radial Acceleration Relation**



240 galaxies; 9 dex in stellar mass

Empirical relation between

- Predicted acceleration from baryons + models
- Measured acceleration from kinematics
- Support modified gravity? MOND (Milgrom 1983)

# Summary

 Galaxy dynamical models Based on integral-field stellar kinematics Demonstrate dichotomy of galaxy properties Indicative of two evolutionary channels Measure nearly universal density profiles Consistent with ACDM paradigm But surprising link of baryons and dark matter